

What makes the proton spin?

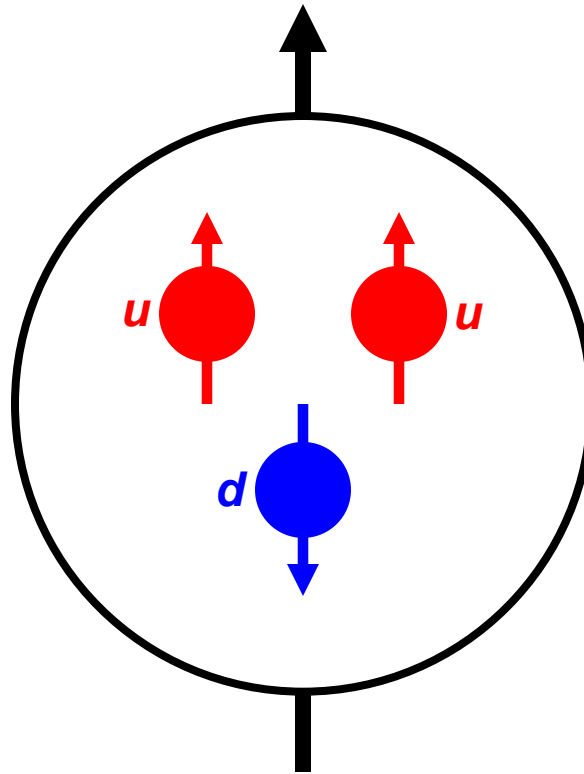
Carl Gagliardi

Texas A&M University

Outline

- Why do we care about the proton spin?
- How do we study it?
- What are we learning?

The proton in the quark model



- We've known that the proton is made of quarks since the 1960's
- The 2 up quarks and 1 down quark together explain the proton quantum numbers: charge, parity, *spin*, ...
- **Spin** is a particularly useful tool to explore the proton structure because it arises from **intrinsic quantum mechanical dynamics**

Proton wavefunction in the static quark model

$$\begin{aligned} & \sqrt{\frac{2}{9}} |(u \uparrow)(u \uparrow)(d \downarrow)\rangle - \sqrt{\frac{1}{18}} |(u \uparrow)(u \downarrow)(d \uparrow)\rangle - \sqrt{\frac{1}{18}} |(u \downarrow)(u \uparrow)(d \uparrow)\rangle + \\ & \sqrt{\frac{2}{9}} |(d \downarrow)(u \uparrow)(u \uparrow)\rangle - \sqrt{\frac{1}{18}} |(d \uparrow)(u \uparrow)(u \downarrow)\rangle - \sqrt{\frac{1}{18}} |(d \uparrow)(u \downarrow)(u \uparrow)\rangle + \\ & \sqrt{\frac{2}{9}} |(u \uparrow)(d \downarrow)(u \uparrow)\rangle - \sqrt{\frac{1}{18}} |(u \downarrow)(d \uparrow)(u \uparrow)\rangle - \sqrt{\frac{1}{18}} |(u \uparrow)(d \uparrow)(u \downarrow)\rangle \end{aligned}$$

x (totally anti-symmetric color wavefunction)

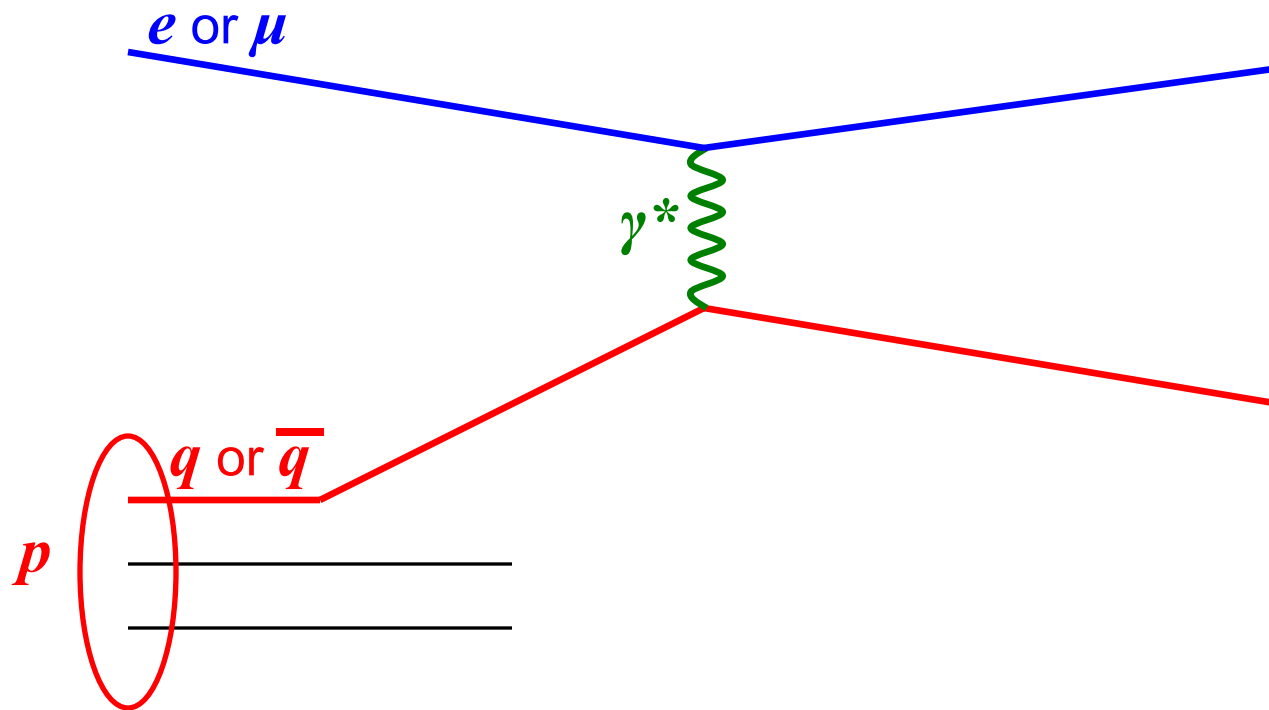
- If $m_u = m_d = m_p/3$. Then:
- Proton magnetic moment:
 - Calculate $+3 \mu_N$; find $+2.793 \mu_N$
- Neutron magnetic moment:
 - Calculate $-2 \mu_N$; find $-1.913 \mu_N$
- Ratio matches prediction to $\sim 3\%$

If assume quarks are slightly heavier to allow for some binding energy, can match the observed magnetic moments very well

Too good to be true

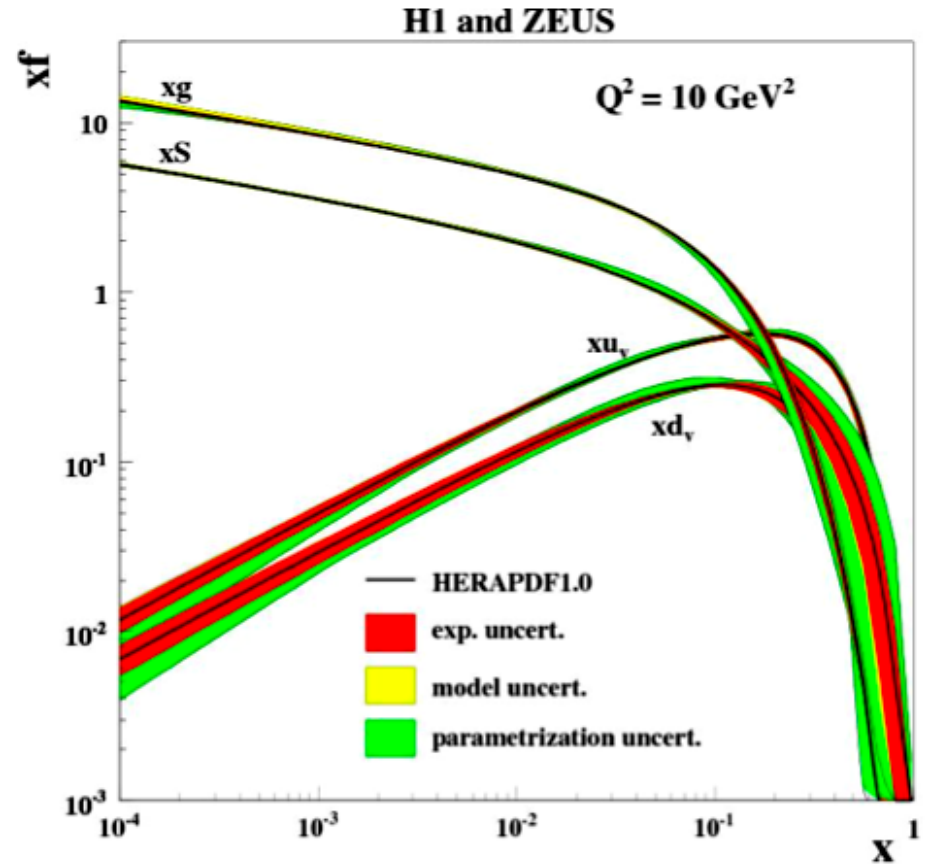
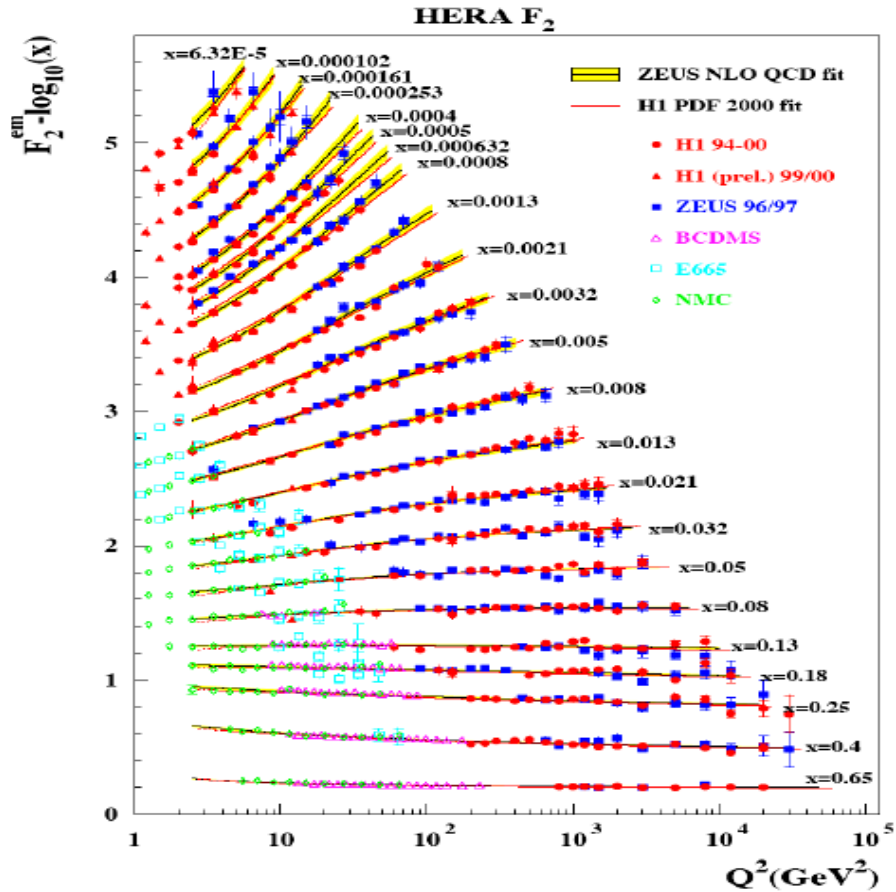
- The proton radius is ~ 0.85 fm
- Heisenberg Uncertainty Principle implies quark motion must be relativistic
- Relativistic quark model
 - Quarks are no longer restricted to s -wave states
 - Quark spin accounts for $\sim 60\%$ of the proton spin
 - Rest of proton spin comes from quark orbital angular momentum
- No binding force in these calculations
- Strong force (Quantum Chromodynamics) provides the quark binding
 - Gluons must also be present
 - Can also have additional quark-antiquark pairs
- **How can we observe these quarks, antiquarks, and gluons?**

Looking inside the proton



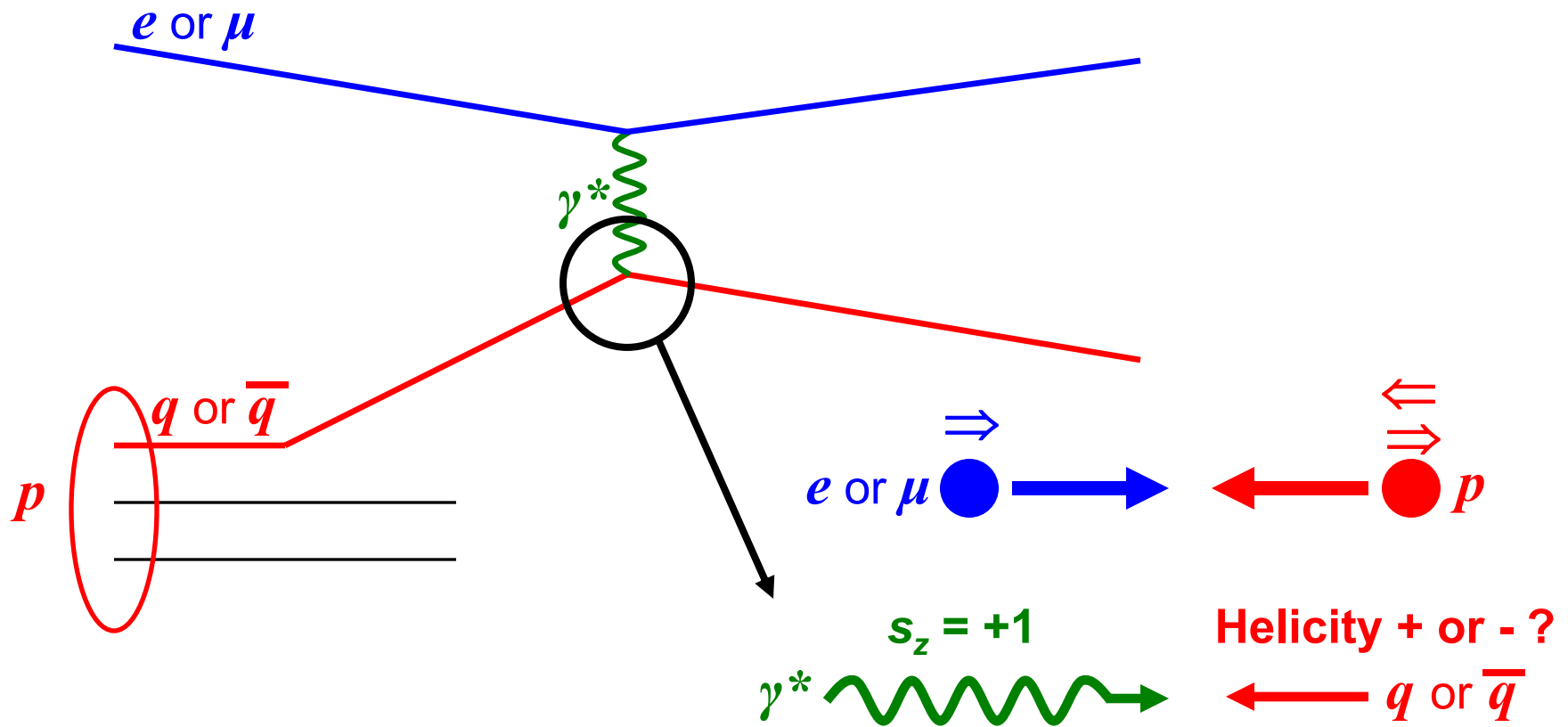
- “Deep-inelastic scattering” (DIS) of electrons and muons off protons has taught us a great deal about the internal structure of the proton
- Interaction is electromagnetic \rightarrow only quarks and anti-quarks participate directly
- Obtain information about gluons indirectly

Parton distribution functions



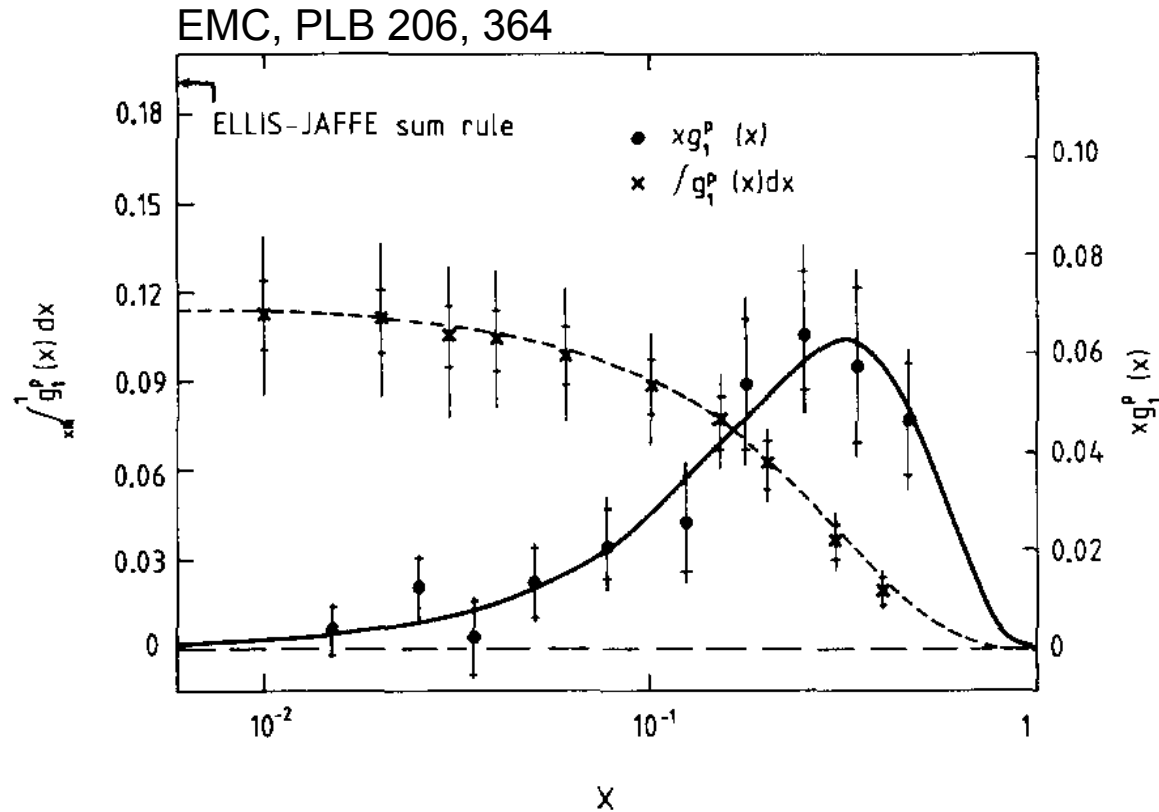
- Probability of finding a quark or gluon inside the proton carrying a fraction x of the total momentum of the proton
- Find **more gluons** than anything else
- Gluons carry **half the momentum** of the proton

Microscopic origin of the proton spin



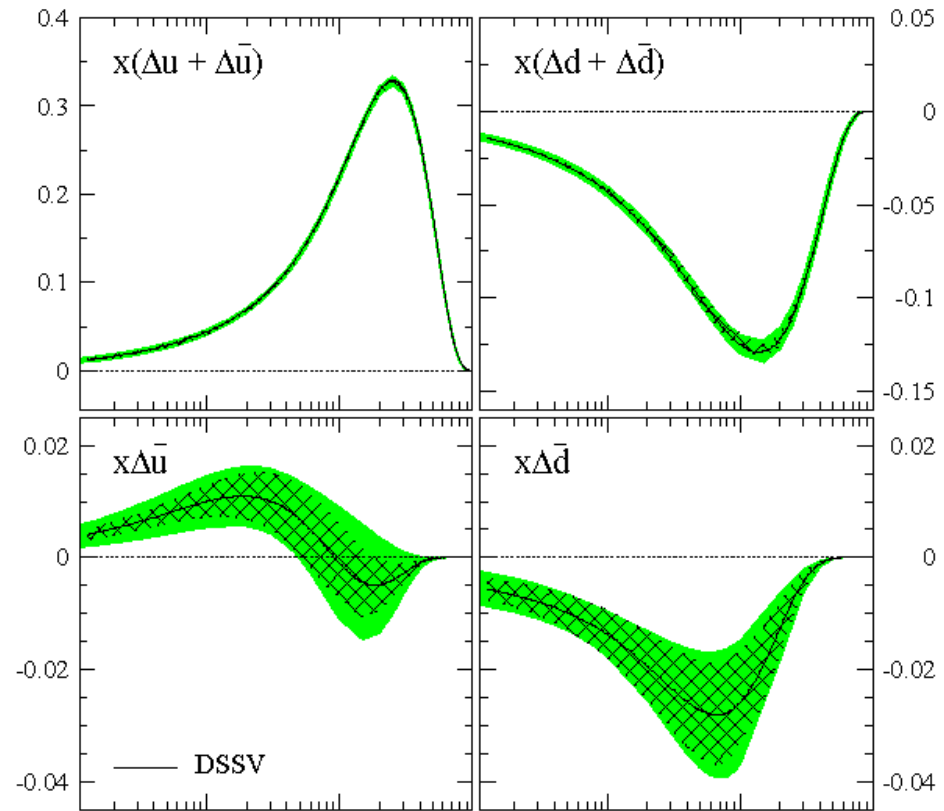
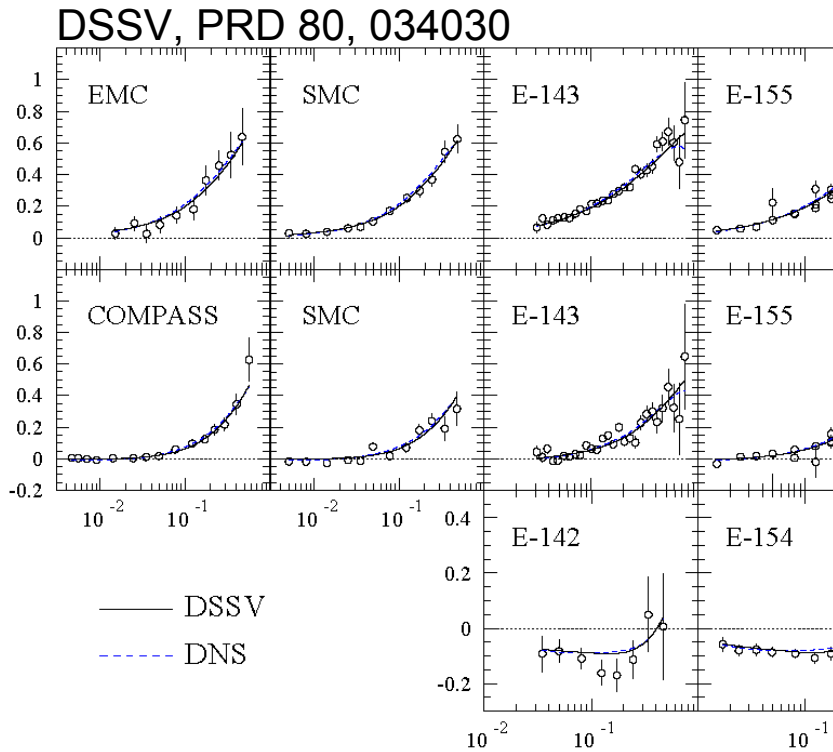
- Measure deep-inelastic scattering with **polarized** electrons or muons off **polarized** protons
- Difference in cross section for like vs. unlike helicity beams provides information about **spin orientations** of the quarks inside the **polarized proton**

Proton “spin crisis”



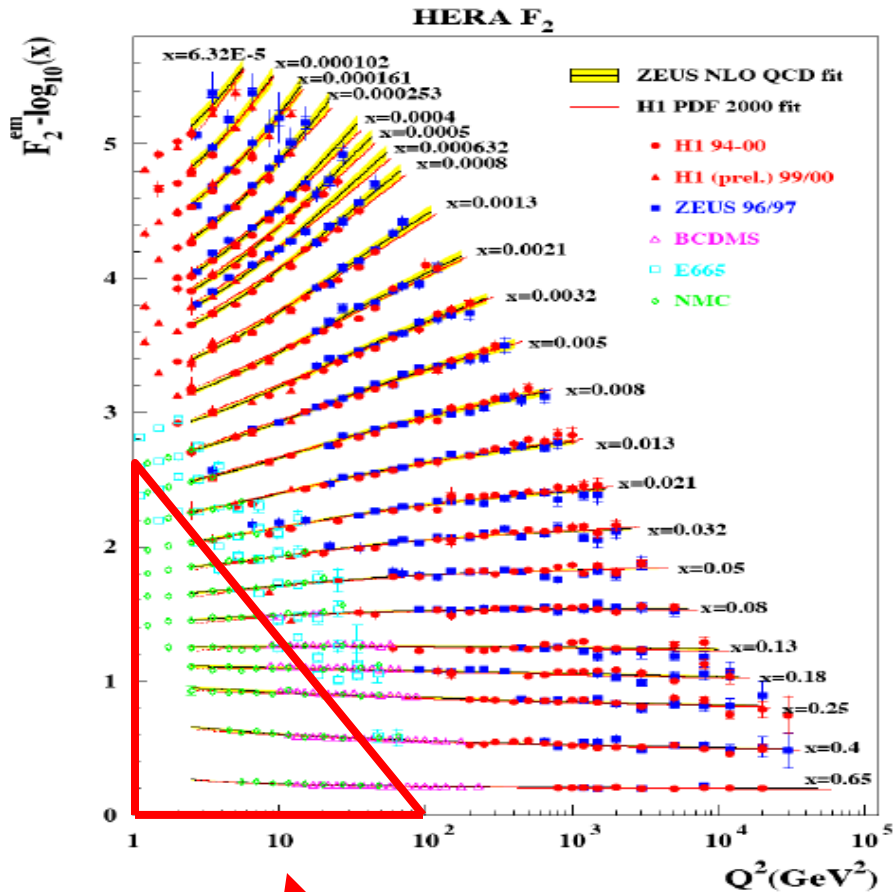
- First measurement over a broad kinematic region was performed by the European Muon Collaboration in the mid-'80s
- Found that quarks contribute only $(14 \pm 9 \pm 21)\%$ of the proton spin

Since EMC

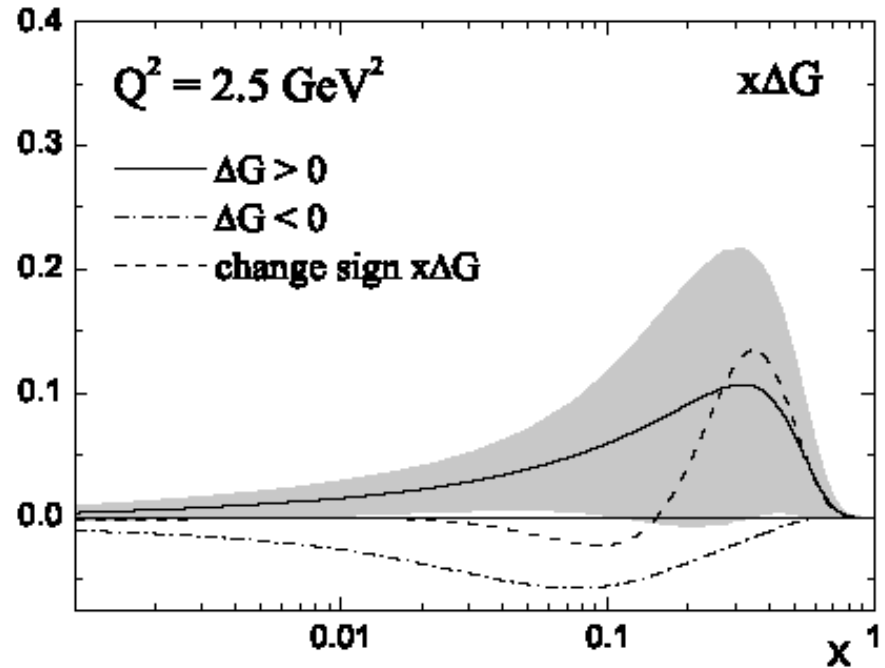


- Many subsequent measurements
- Results are well described by “global analyses” that find best-fit *polarized parton distribution functions*
- Polarization of $u+\bar{u}$ and $d+\bar{d}$ quarks well determined
 - Individual u , \bar{u} , d , \bar{d} polarizations have much larger uncertainty
- Only **~30% of the proton spin** arises from quarks and antiquarks

What about gluon polarization?



Kinematic region of **polarized** measurements



Three fits of equal quality:

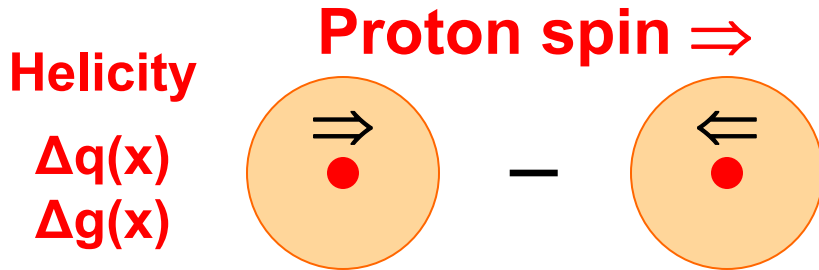
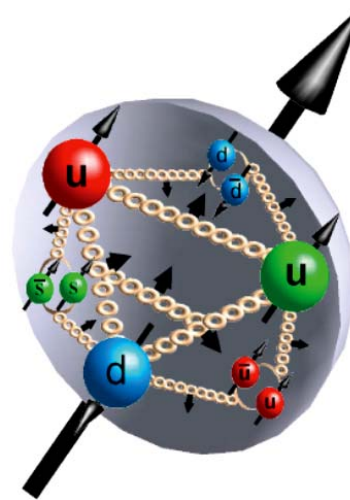
- $\Delta G = 0.13 \pm 0.16$
- $\Delta G \sim 0.006$
- $\Delta G = -0.20 \pm 0.41$

all at $Q^2 = 1 \text{ GeV}^2$

Leader et al, PRD 75, 074027

What contributes to the proton spin?

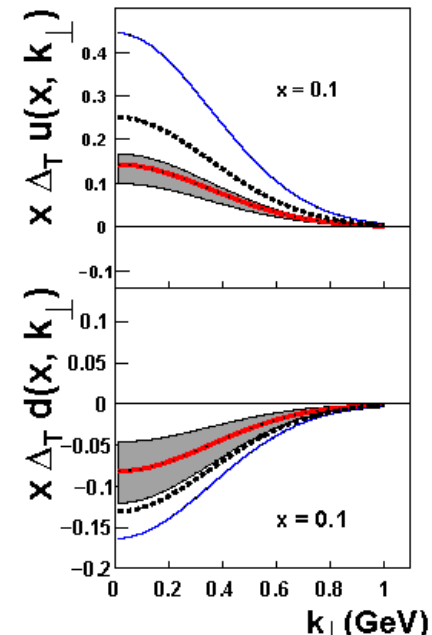
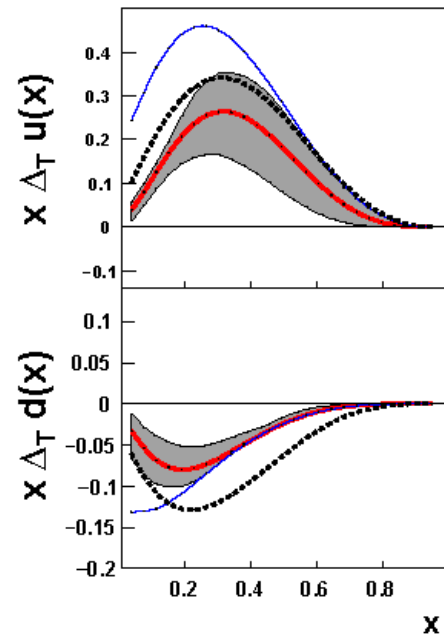
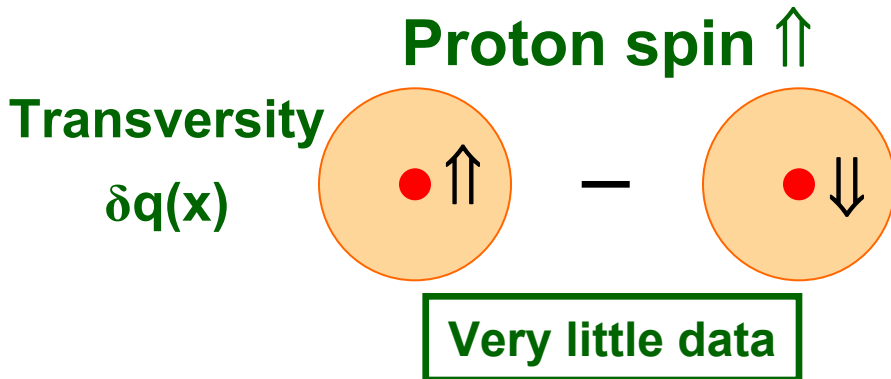
Consider a proton moving toward the right



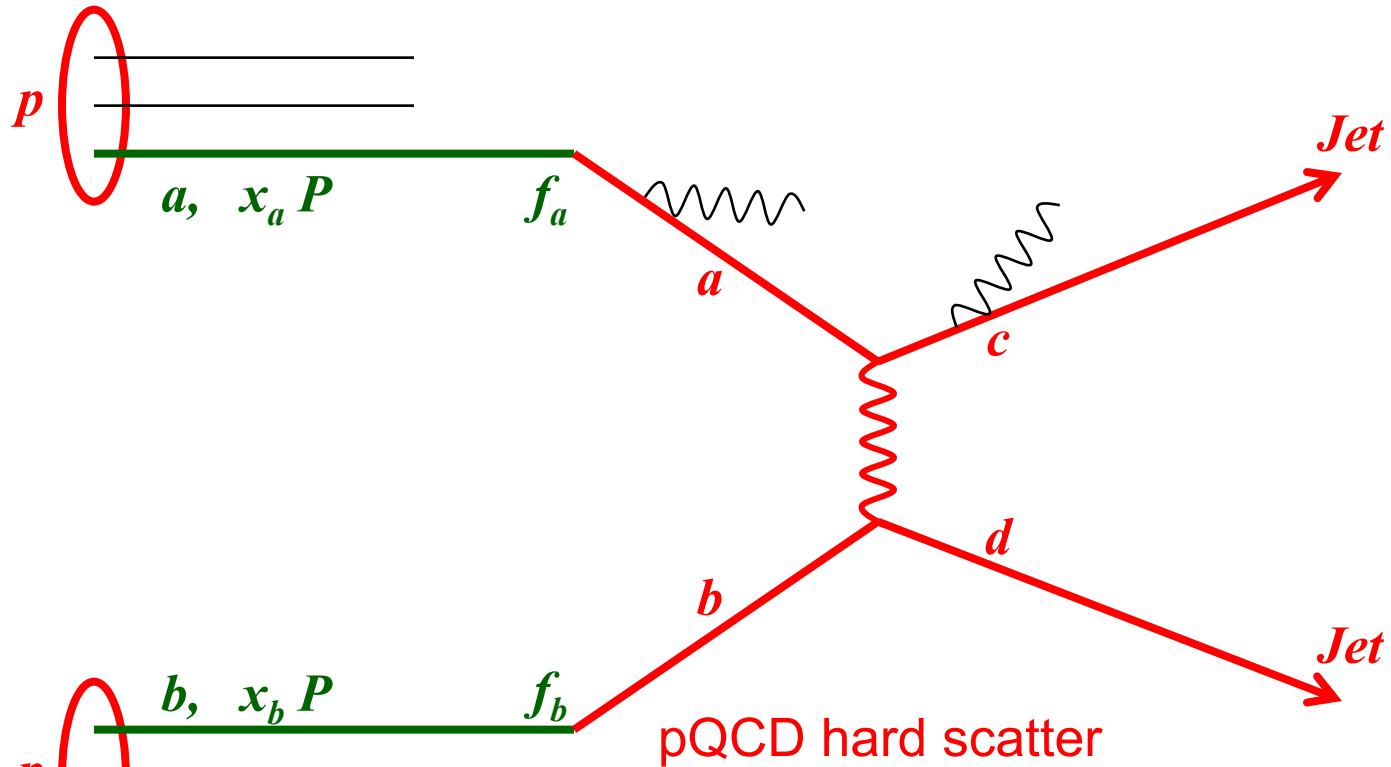
Polarized DIS: ~ 0.3

Poorly Anselmino et al, arXiv:0812.4366

Spin sum rule: $\langle S_z^P \rangle = \frac{1}{2} = \frac{1}{2} \Delta \Sigma$



$p + p$ collisions in perturbative QCD



$$\sigma = \sum f_a(x_a, Q^2) f_b(x_b, Q^2) \hat{\sigma}_{a+b \rightarrow c+d}$$

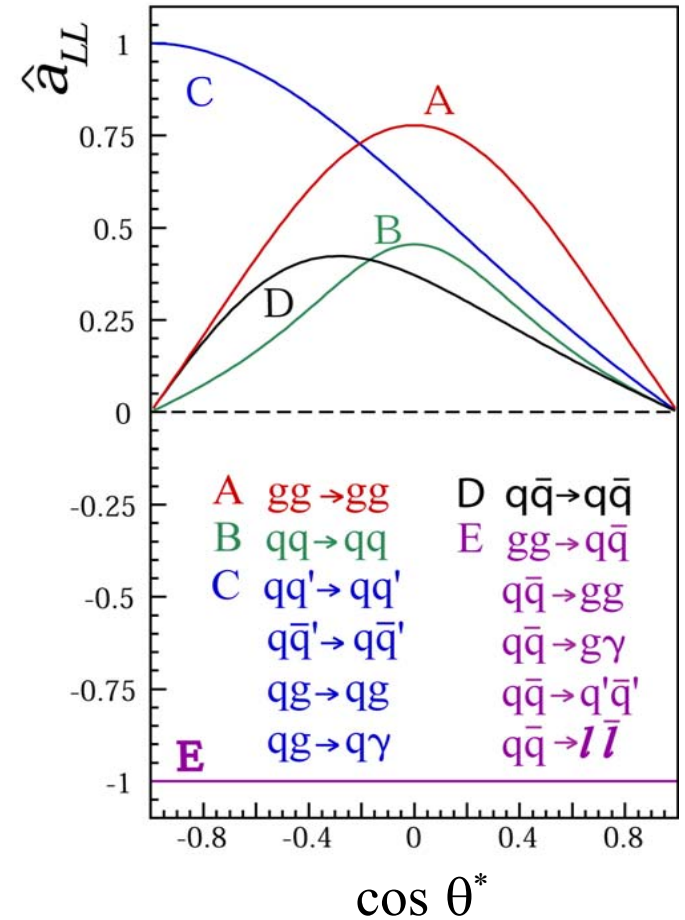
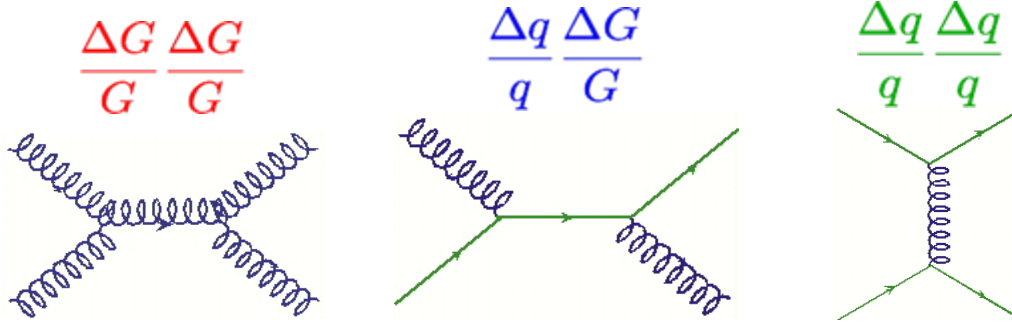
Parton distribution functions

a and b can be quarks, gluons, or a combination

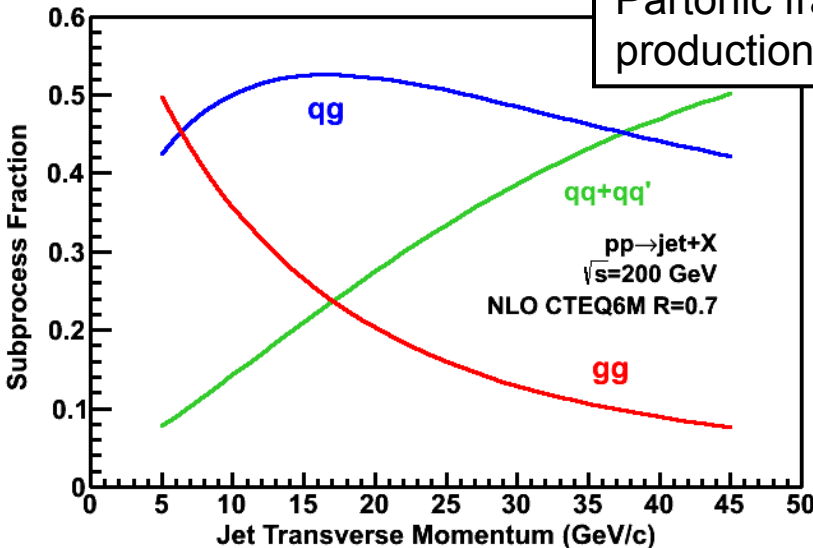
Exploring gluon polarization at RHIC

$$A_{LL} = \frac{\sigma^{++} - \sigma^{+-}}{\sigma^{++} + \sigma^{+-}} \propto \frac{\Delta f_a \Delta f_b}{f_a f_b} \hat{a}_{LL}$$

Δf : polarized parton distribution functions

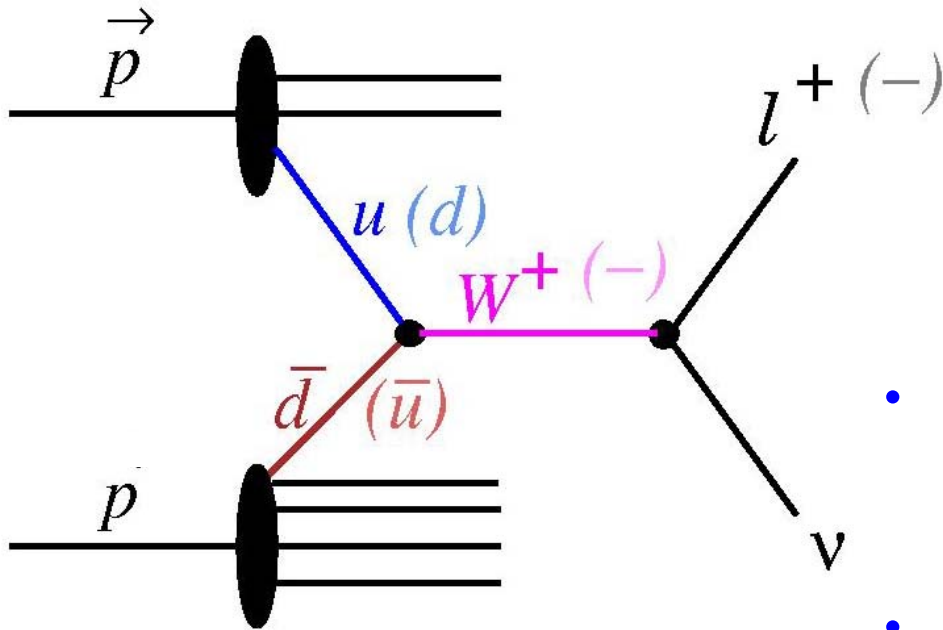


Partonic fractions in jet production at 200 GeV



For most RHIC kinematics, **gg** and **qg** dominate, making A_{LL} sensitive to **gluon polarization**.

Separating quark and anti-quark polarizations



$$u + \bar{d} \rightarrow W^+ \rightarrow e^+ + \nu$$

$$\bar{u} + d \rightarrow W^- \rightarrow e^- + \bar{\nu}$$

- Weak interaction process
 - Only left-handed quarks
 - Only right-handed anti-quarks
- Perfect spin separation

Measure parity violating single helicity asymmetry A_L
 (Helicity flip in one beam while averaging over the other)

$$A_L^{W^-} \propto -\Delta d(x_1)\bar{u}(x_2) + \Delta\bar{u}(x_1)d(x_2) \quad A_L^{W^+} \propto -\Delta u(x_1)\bar{d}(x_2) + \Delta\bar{d}(x_1)u(x_2)$$

What's needed to determine A_{LL} ?



N_{++} : yield when helicities same

Versus



N_{+-} : yield when helicities opposite

$$A_{LL} = \frac{1}{P_1 P_2} \frac{N_{++} - RN_{+-}}{N_{++} + RN_{+-}} \quad \text{where} \quad R = \frac{L_{++}}{L_{+-}}$$

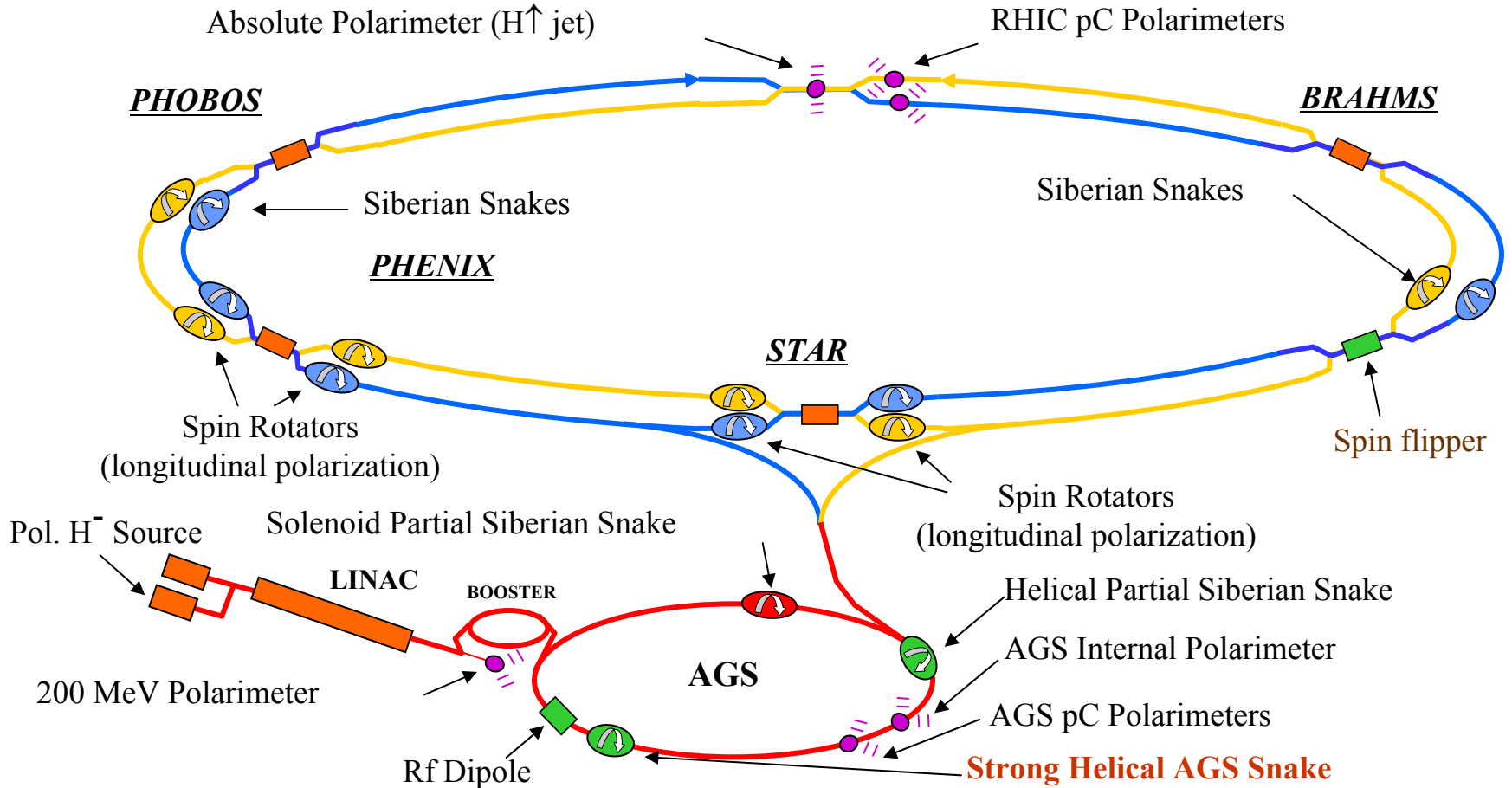
- Three concurrent measurements:
 - Beam polarizations
 - Relative luminosities
 - Event yields
- A_L is done similarly, but with one beam polarized and one unpolarized

RHIC: the Relativistic Heavy Ion Collider



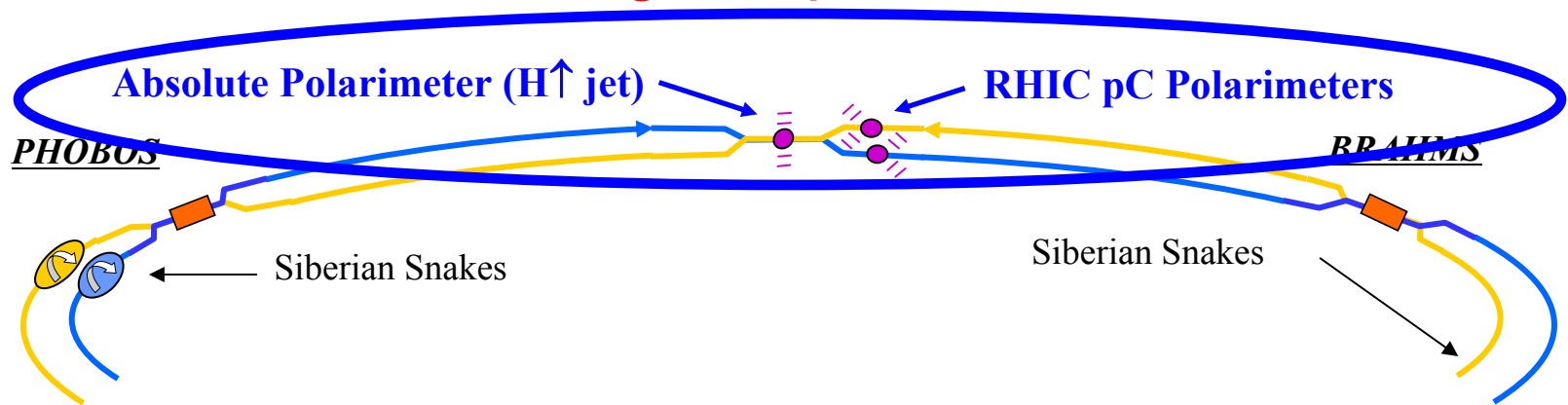
- Search for and study the Quark-Gluon Plasma
- **Explore the partonic structure of the proton**
- Determine the partonic structure of nuclei

RHIC: the world's first (and only!) polarized hadron collider



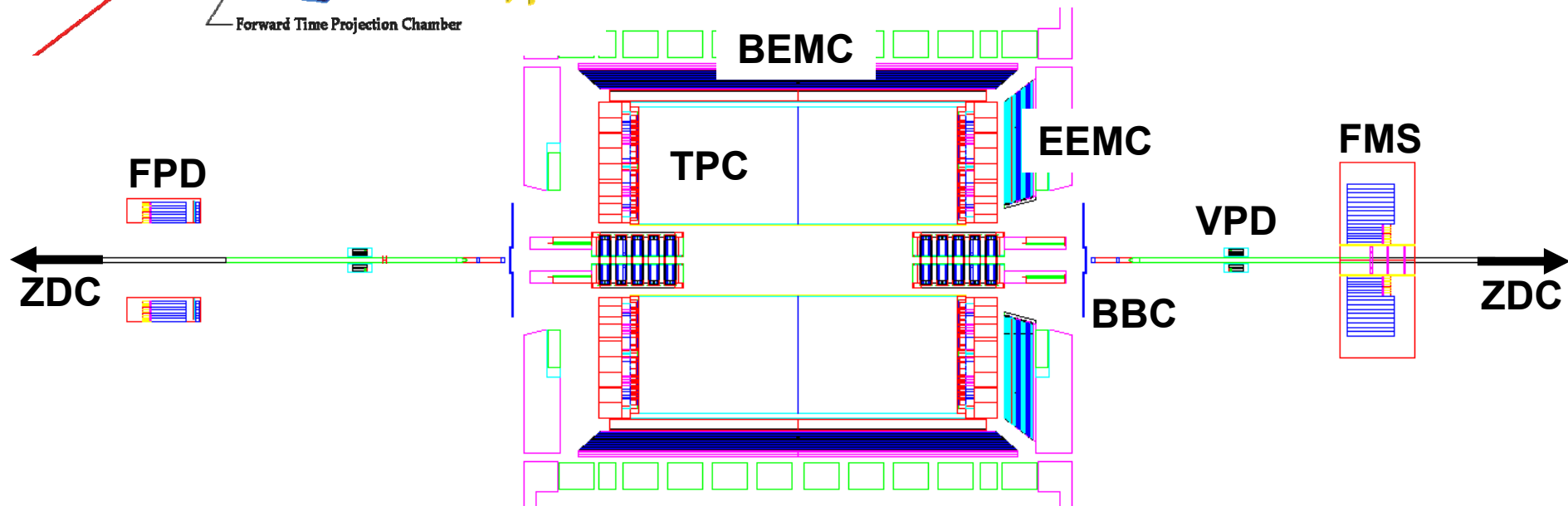
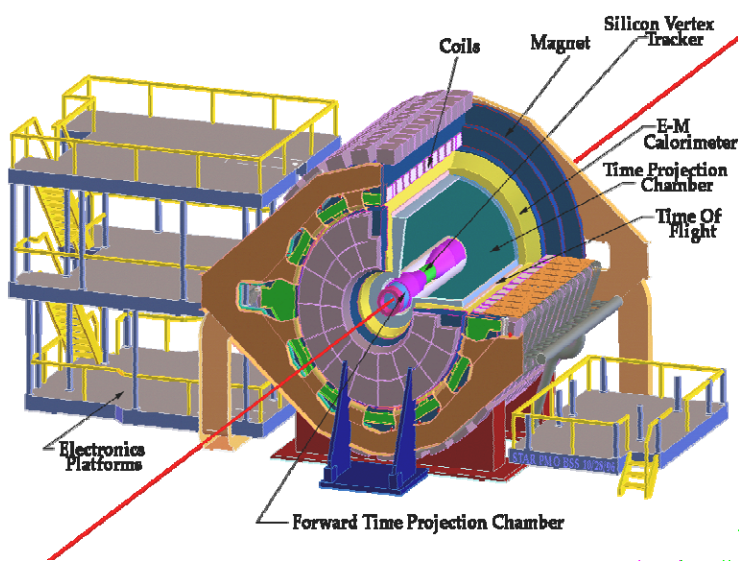
- Spin varies from rf bucket to rf bucket (9.4 MHz)
- Spin pattern changes from fill to fill
- Spin rotators provide choice of spin orientation
- Billions of spin reversals during a fill with little depolarization

Measuring the polarization



- p-Carbon
 - Quick measurements
 - Determine beam polarization and intensity profiles
 - Multiple measurements give time dependence during a fill
 - Only give relative measurements
- H Jet
 - Circulating beams scatter off a polarized H atomic beam
 - Atomic beam polarization known with high precision
 - Provides absolute determination of the circulating beam polarizations averaged over each fill

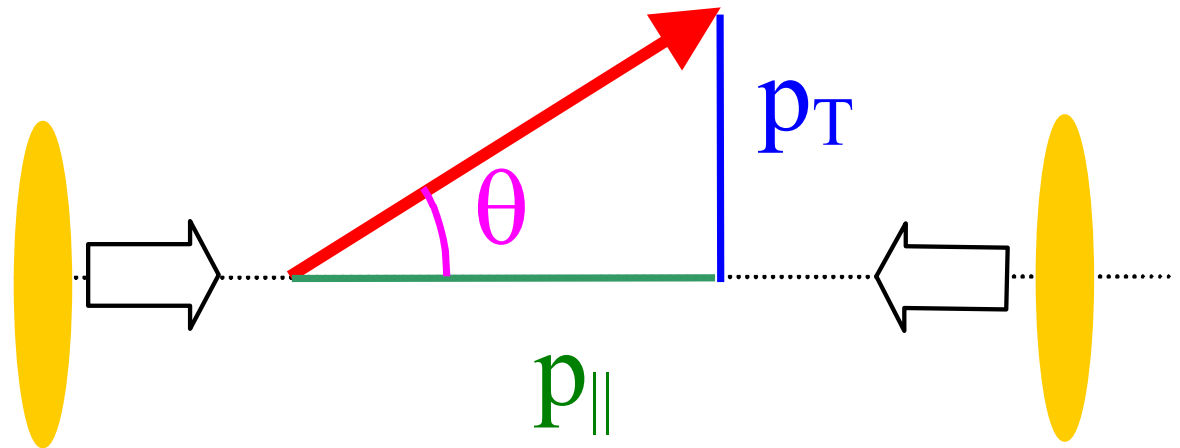
Event yields and luminosity: the *STAR* detector in two views



- High precision tracking with the TPC
- Electromagnetic calorimetry with the BEMC, EEMC, and FMS
- Additional detectors for relative luminosity, local polarimetry, and minbias triggering

What are we learning?

Kinematics for colliders



Pseudo-rapidity: $\eta = -\ln[\tan(\theta/2)]$

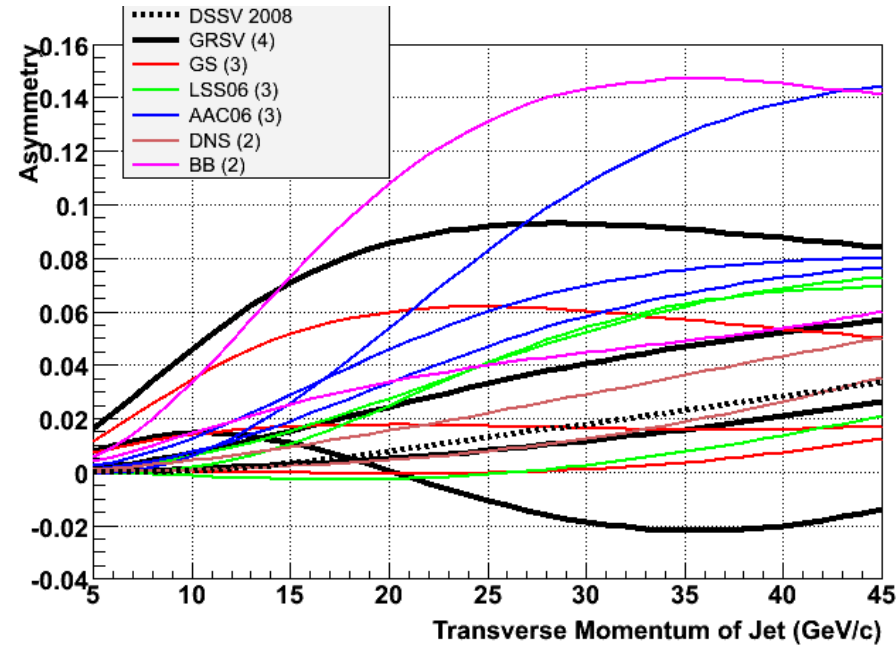
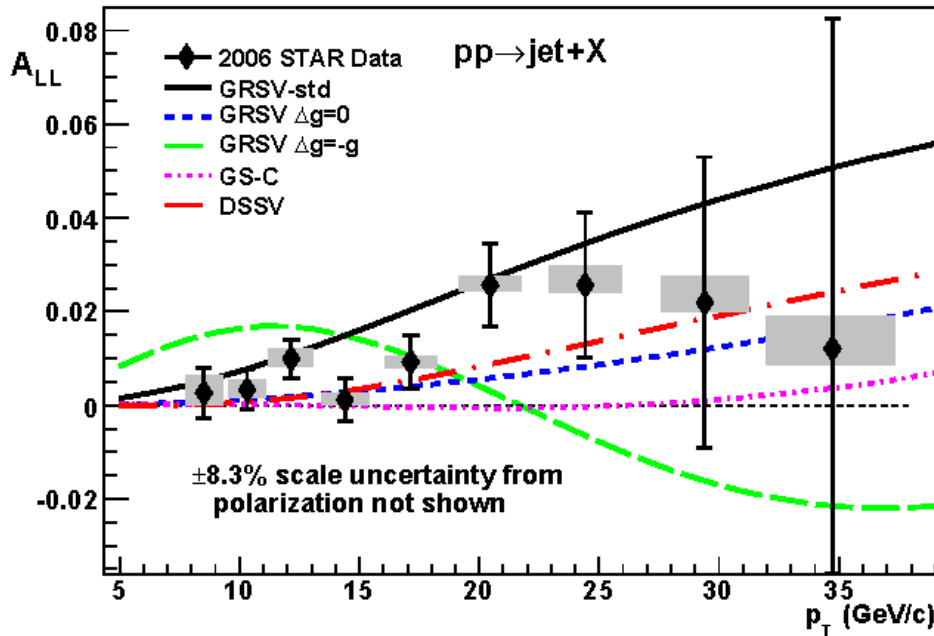
Transverse momentum (p_T) and pseudorapidity (η) provide a convenient description

$$p_z = p_T \sinh(\eta)$$

$$p_{tot} = p_T \cosh(\eta)$$

Mid-rapidity: $\eta = 0$, perpendicular to the incident beams
 $\eta = 1$: Scattering at $\theta \sim 40^\circ$ in the CM (or lab) frame
 $\eta = 2$: Scattering at $\theta \sim 15^\circ$ in the CM (or lab) frame

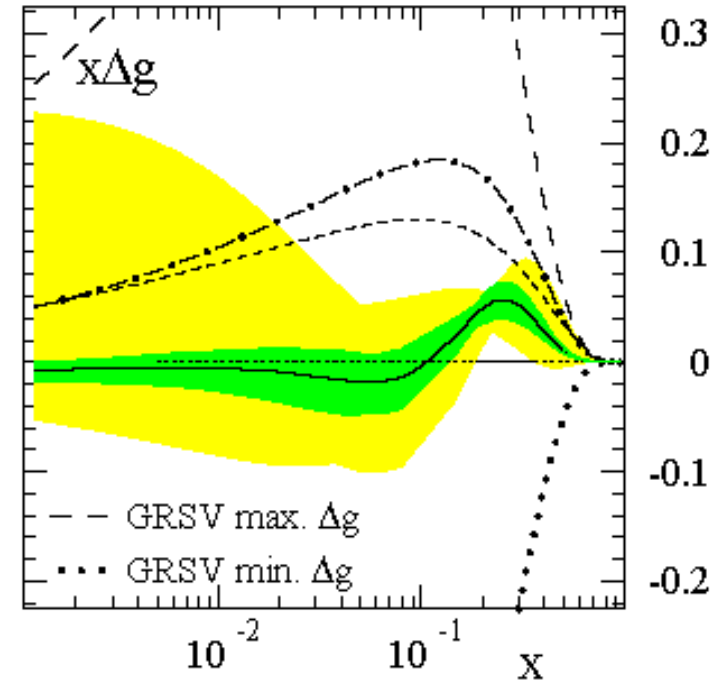
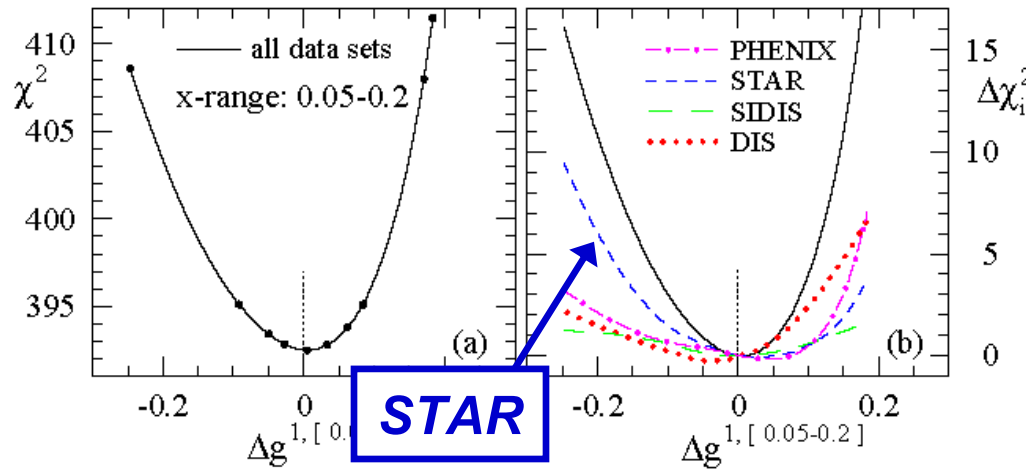
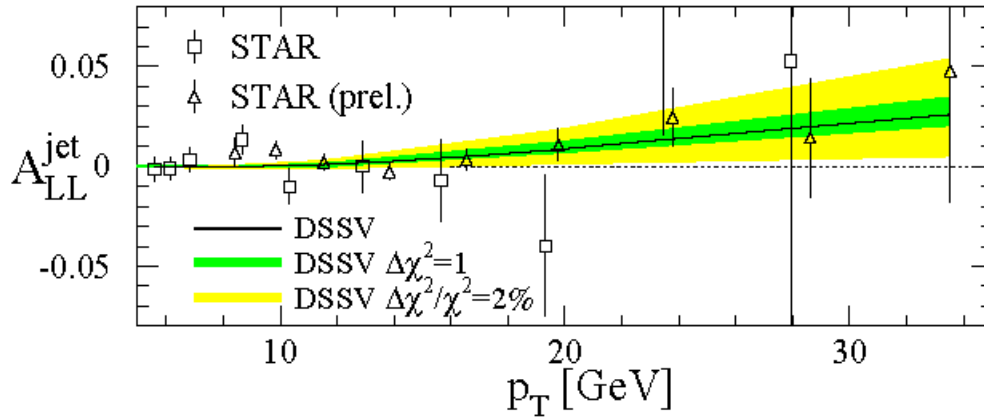
STAR inclusive jet A_{LL} from 2006



- STAR inclusive jet A_{LL} excludes those scenarios that have a large gluon polarization within the accessible x region

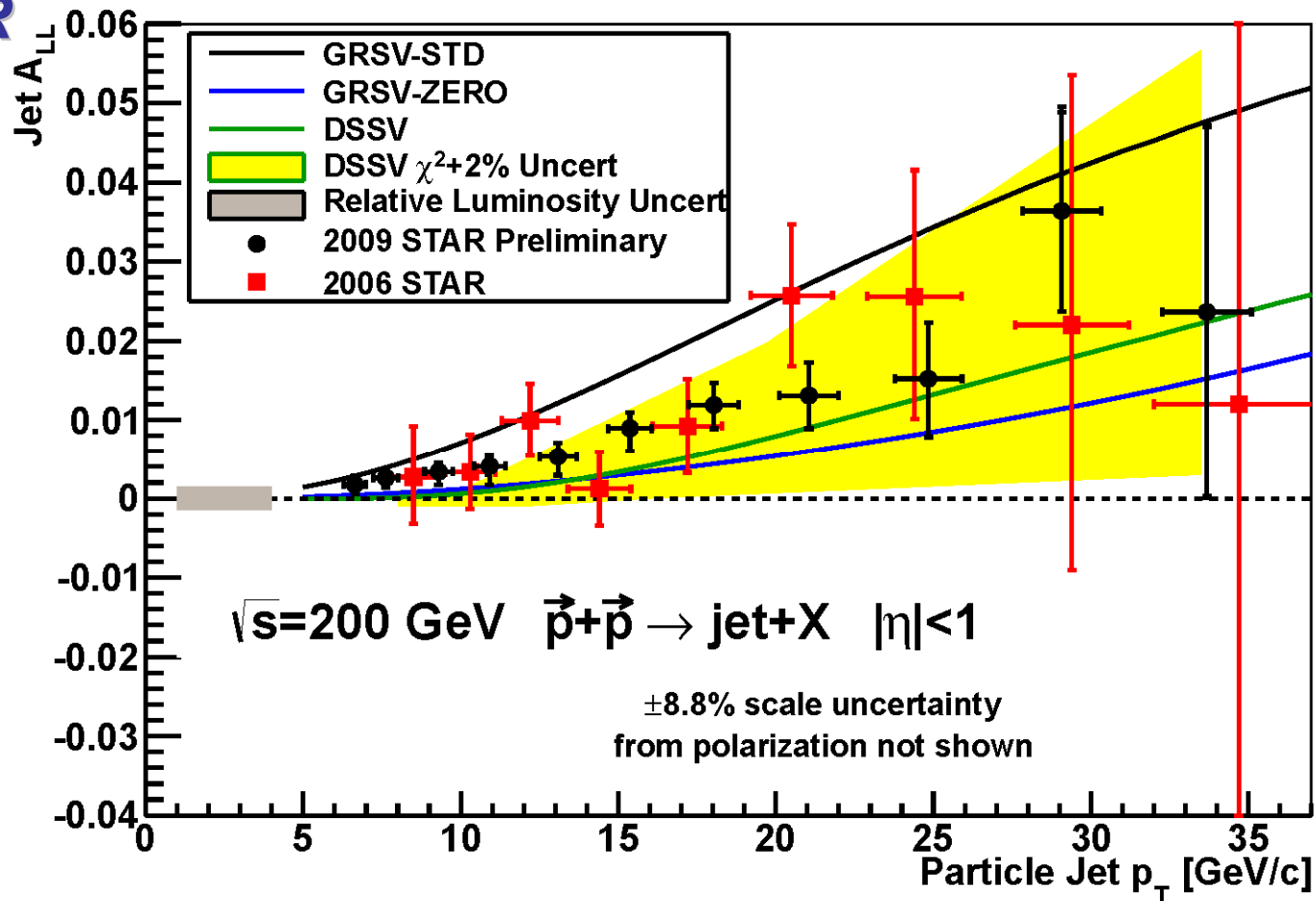
DSSV – first global analysis with polarized jets

de Florian et al., PRL 101, 072001



- The first global NLO analysis to include inclusive DIS, SIDIS, and RHIC pp data on an equal footing

A_{LL} for inclusive jets: 2006 to 2009

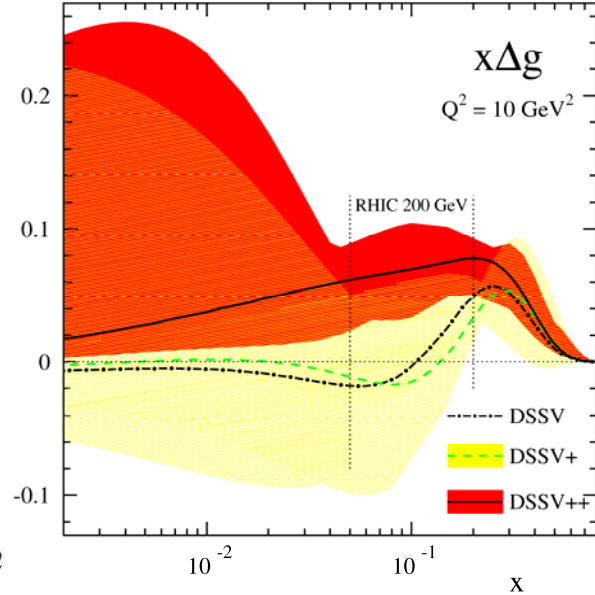
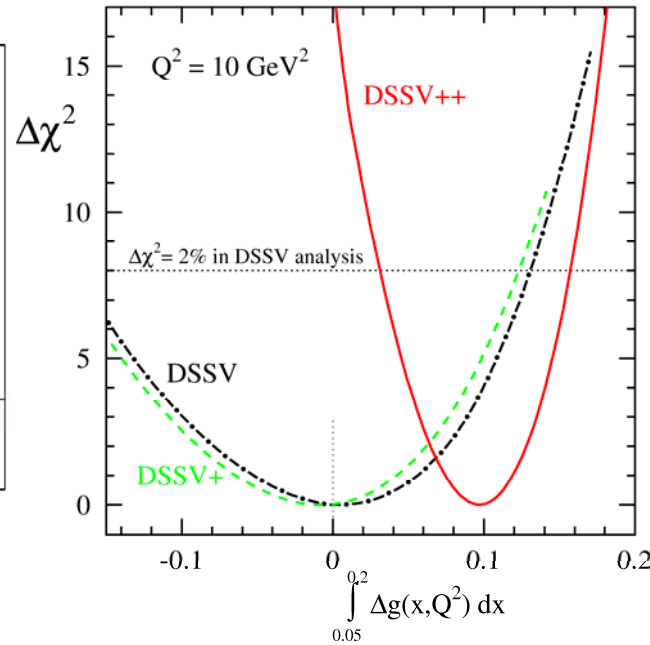
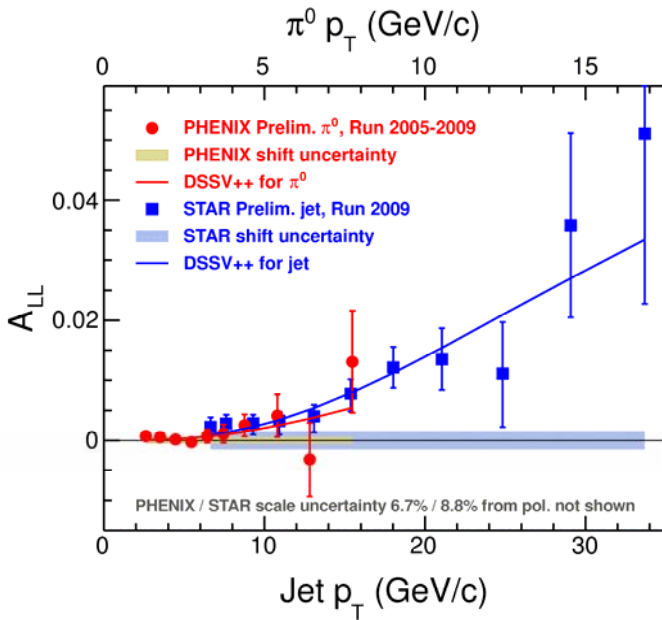


- 2009 **STAR** inclusive jet A_{LL} measurements are a factor of 3 (high- p_T) to >4 (low- p_T) more precise than 2006
- **Results fall between predictions from DSSV and GRSV-STD**

New global analysis with 2009 RHIC data

arXiv:1304.0079

Special thanks to the DSSV group!

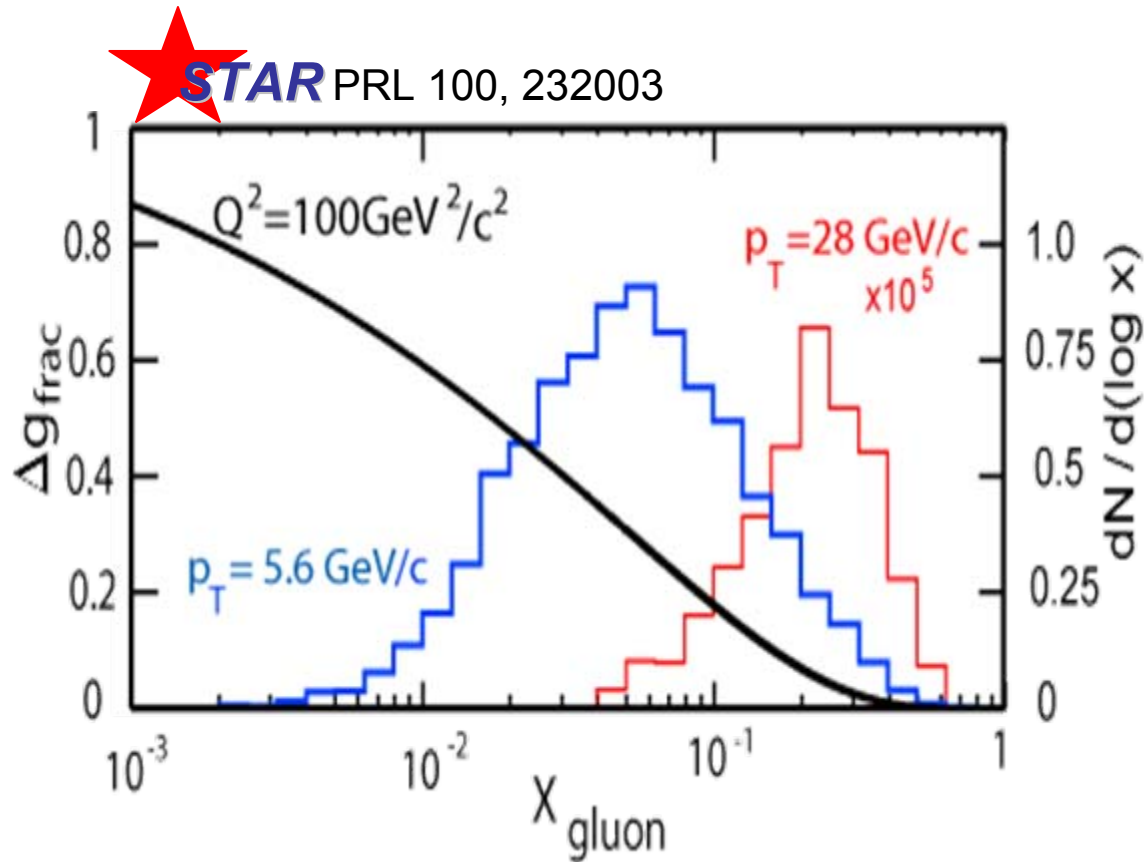


- **DSSV++** is a new, preliminary global analysis from the DSSV group that includes preliminary 2009 A_{LL} measurements from PHENIX and STAR

$$\int_{0.05}^{0.2} \Delta g(x, Q^2 = 10 \text{ GeV}^2) dx = 0.10^{+0.06}_{-0.07}$$

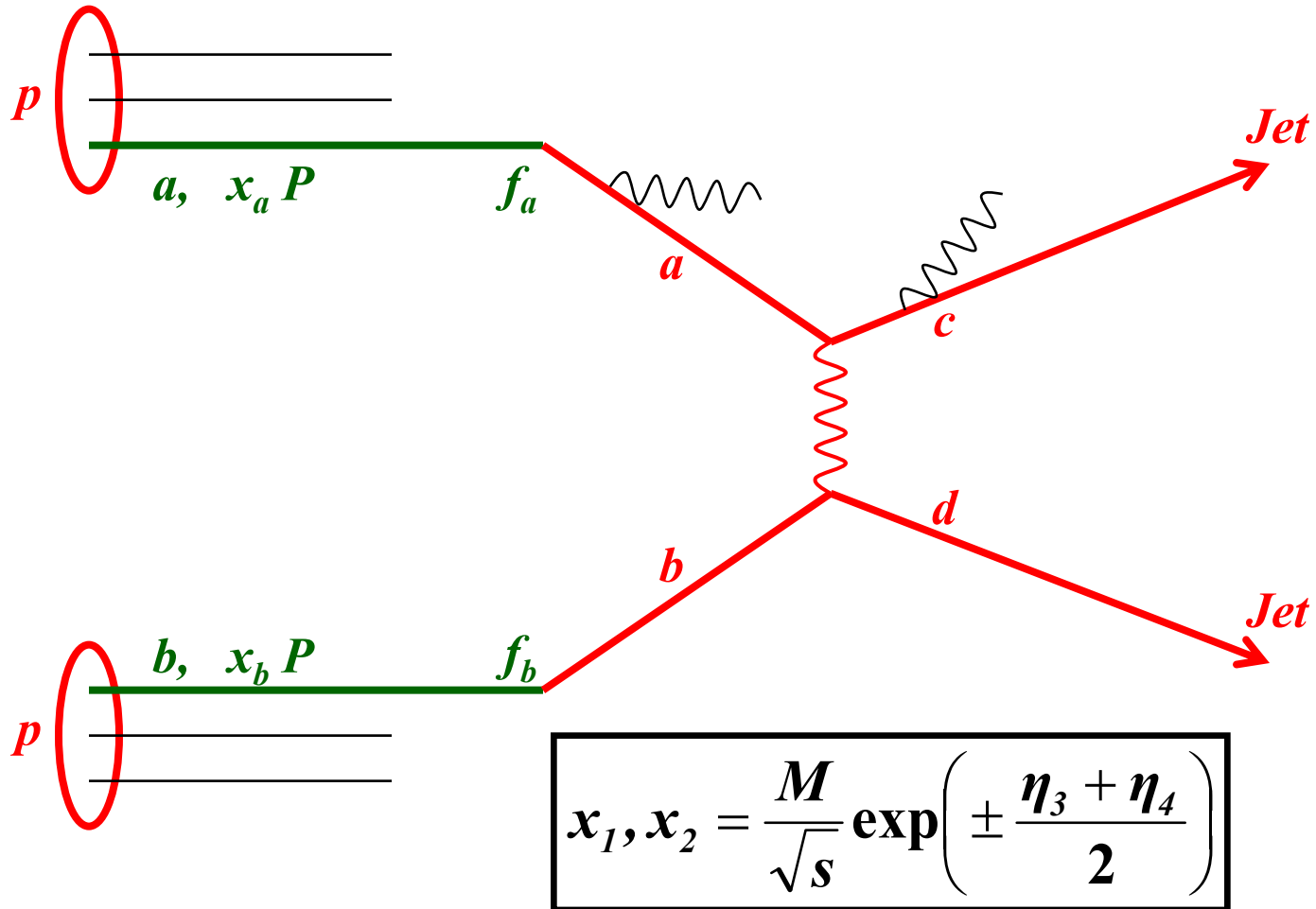
- **First experimental evidence of non-zero gluon polarization in the RHIC range ($0.05 < x < 0.2$)**

Beyond inclusive A_{LL} measurements



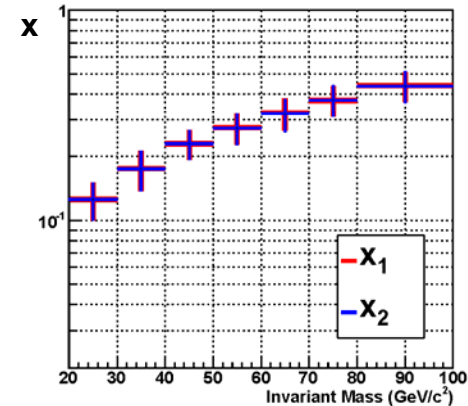
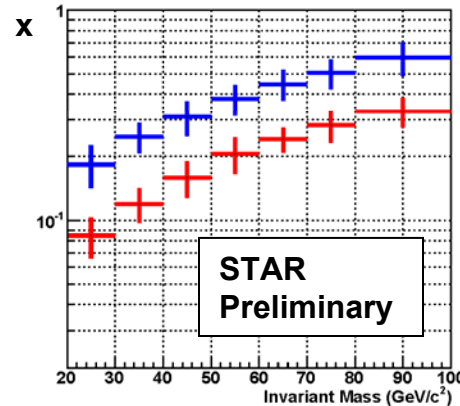
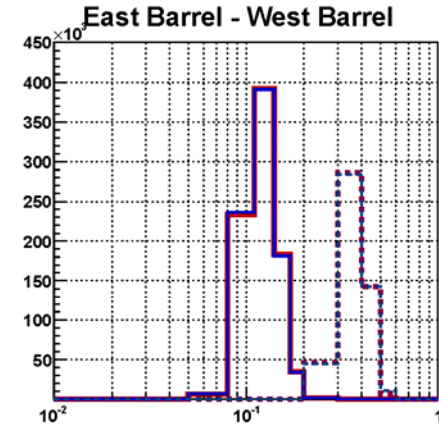
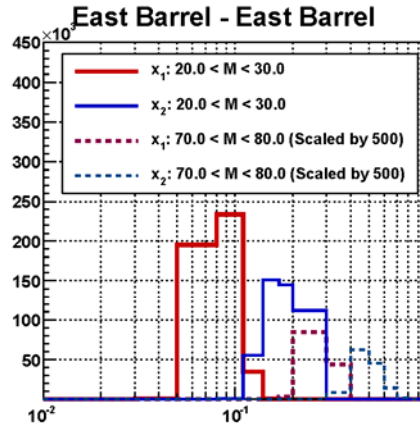
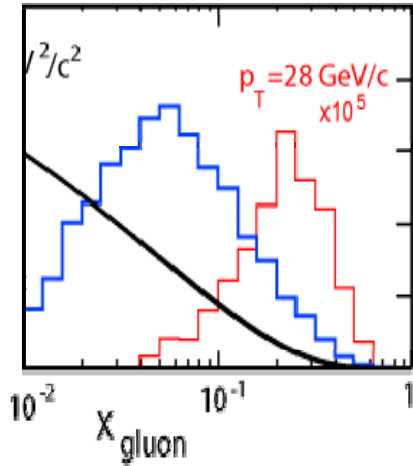
- Inclusive A_{LL} measurements at fixed p_T average over a **broad x range**.
- Can hide considerable structure if $\Delta g(x)$ has a node
- **Di-jet measurements can constrain the shape of $\Delta g(x)$**

$p + p$ collisions in perturbative QCD



- Di-jets provide direct access to parton kinematics at leading order

2009 *STAR* di-jet partonic coverage



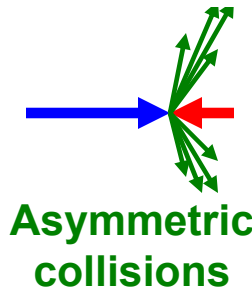
$$x_1 = \frac{1}{\sqrt{s}} (p_{T,3} e^{\eta_3} + p_{T,4} e^{\eta_4})$$

$$x_2 = \frac{1}{\sqrt{s}} (p_{T,3} e^{-\eta_3} + p_{T,4} e^{-\eta_4})$$

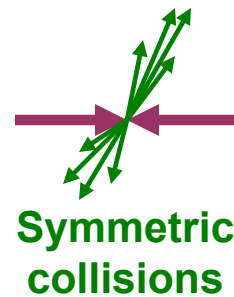
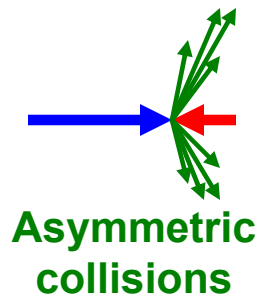
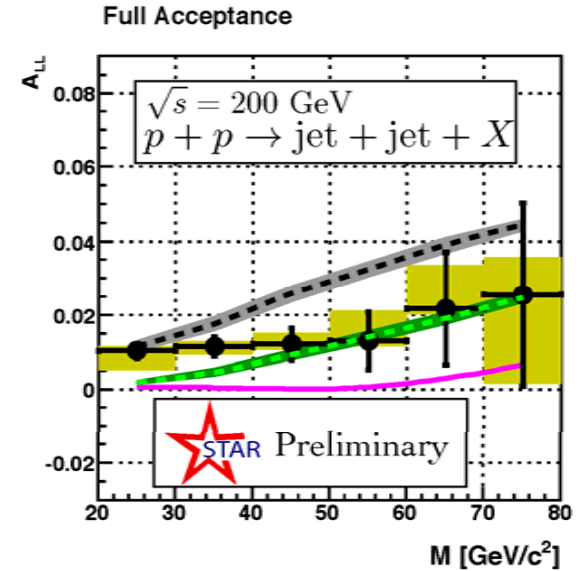
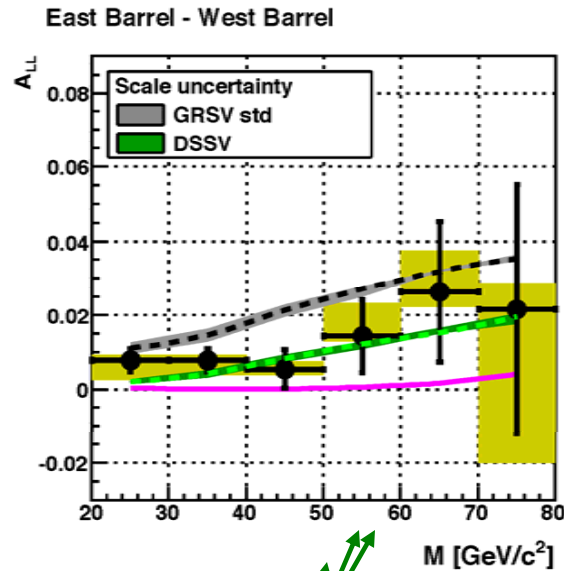
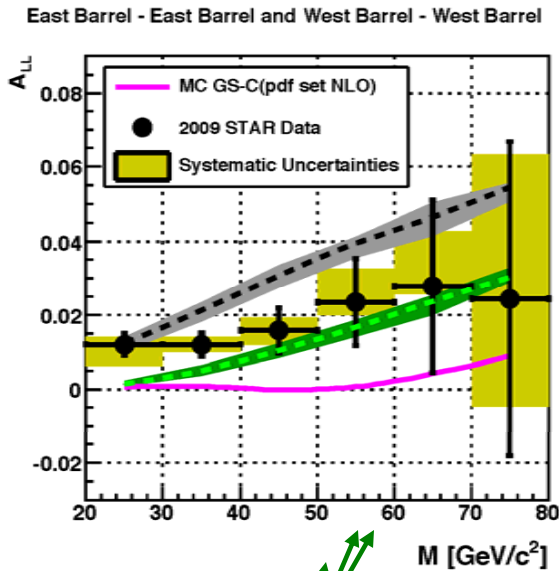
$$M = \sqrt{x_1 x_2 s}$$

$$y = \frac{1}{2} \ln \frac{x_1}{x_2} = \frac{\eta_3 + \eta_4}{2}$$

$$|\cos\theta^*| = \tanh \frac{|\eta_3 - \eta_4|}{2}$$

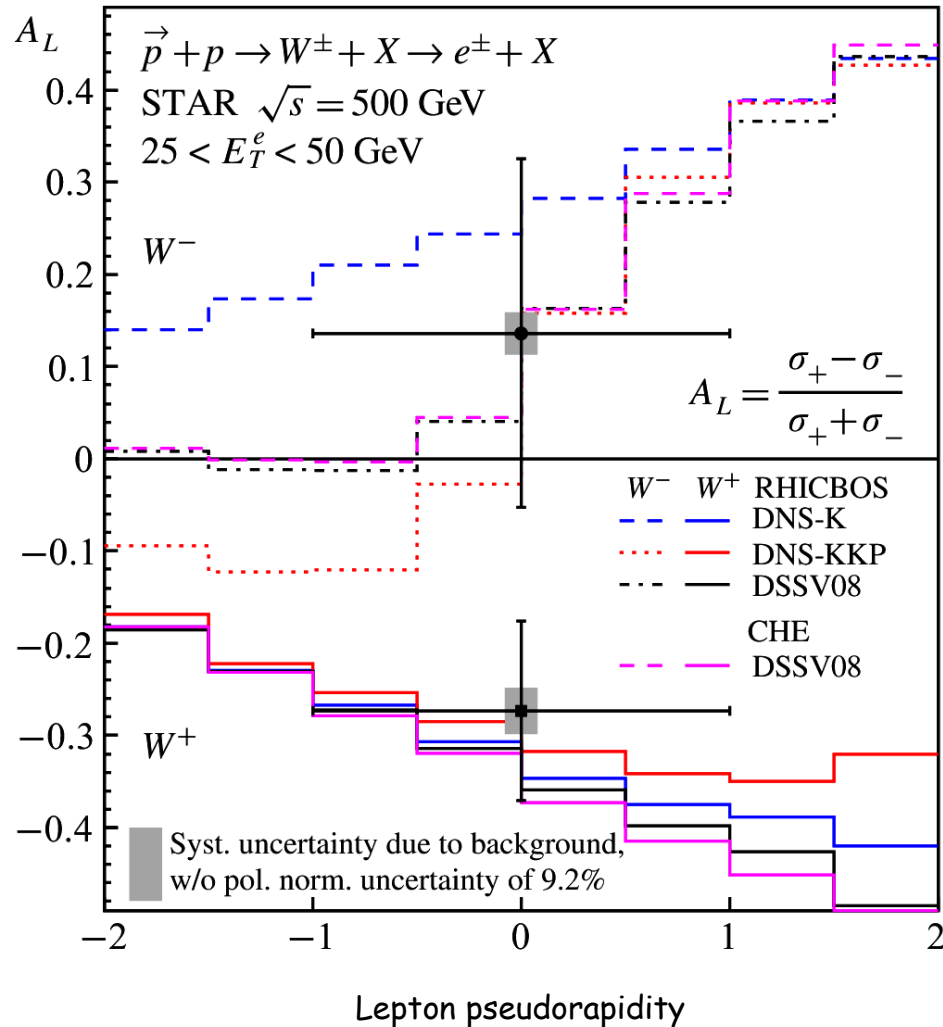


2009 *STAR* di-jet A_{LL}



- For fixed M , different kinematic regions sample different x ranges
- **Results fall between predictions from DSSV and GRSV-STD**

First STAR $W A_L$



$$A_L = \frac{\sigma_+ - \sigma_-}{\sigma_+ + \sigma_-}$$

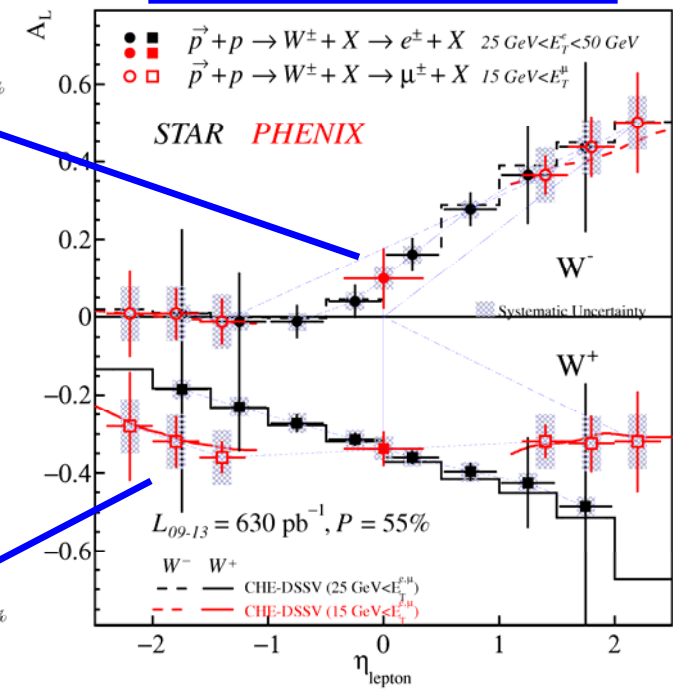
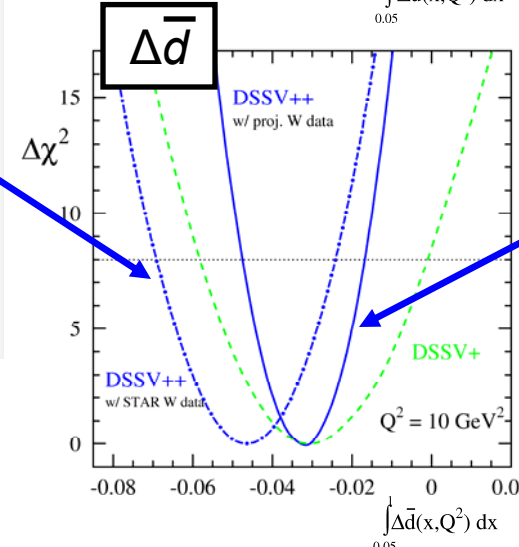
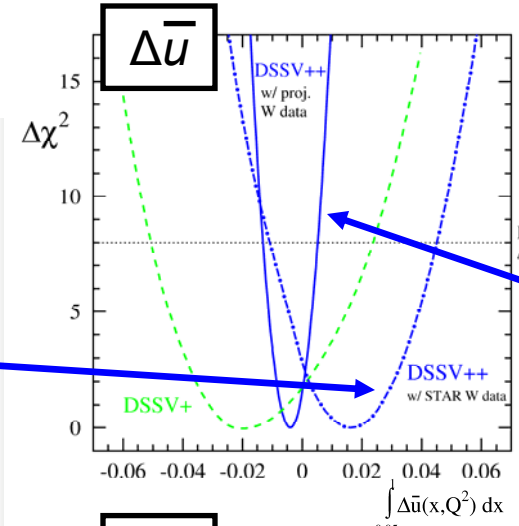
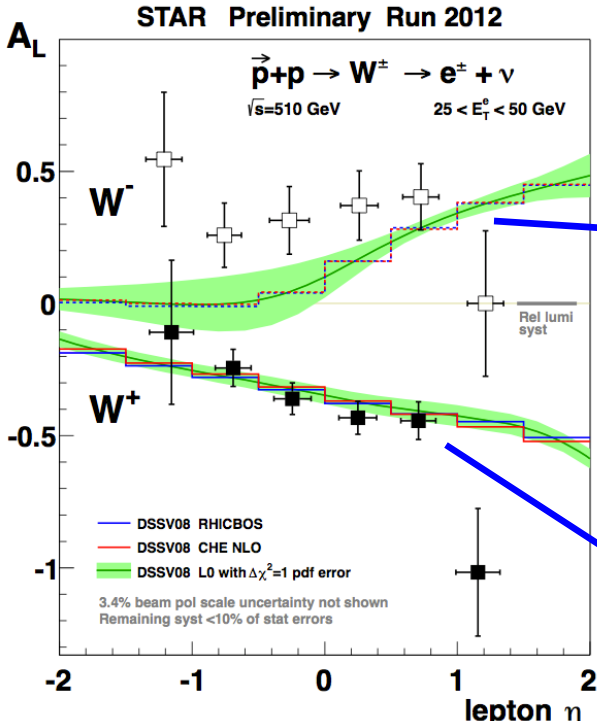
STAR 2009 Result

$$A_L(W^+) = -0.27 \pm 0.10(stat) \pm 0.02(syst)$$

$$A_L(W^-) = 0.14 \pm 0.19(stat) \pm 0.02(syst)$$

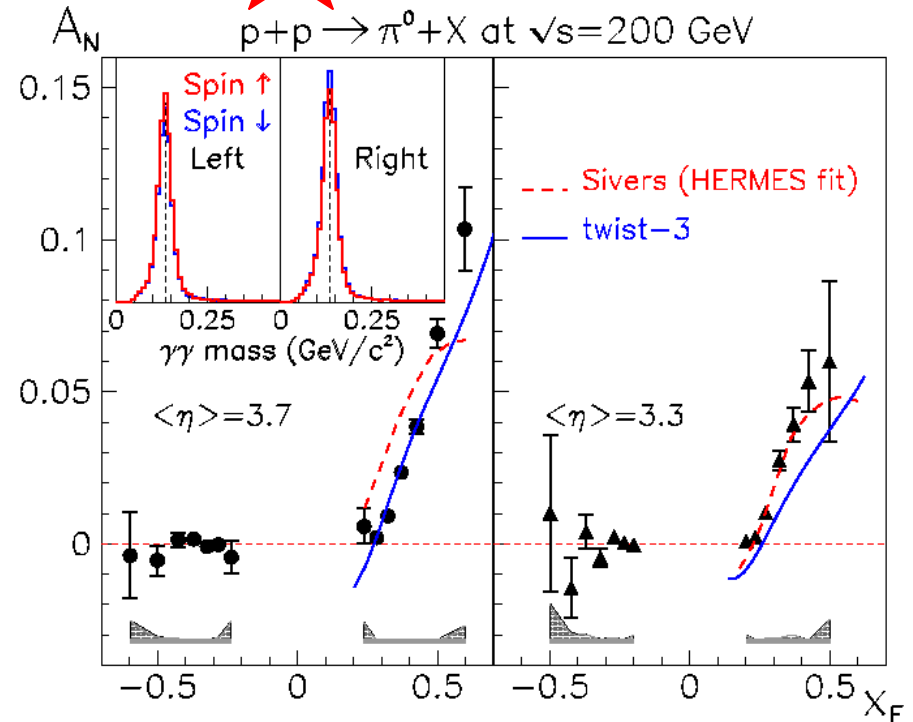
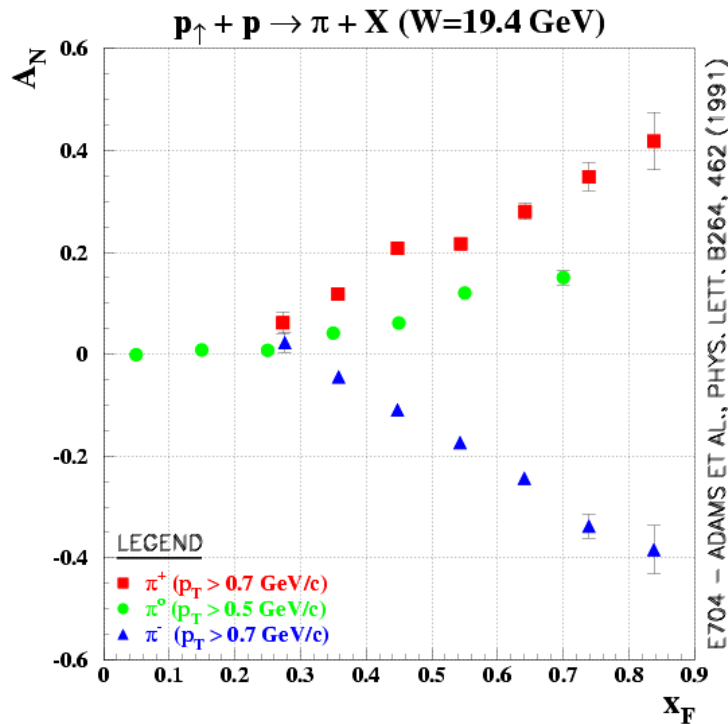
High precision W asymmetry era

PHENIX and STAR
through 2013 run



- First preliminary results from 2012 already provide substantial sensitivity
- Future results will provide a dramatic reduction in the uncertainties

Transverse single-spin asymmetries at forward rapidity



- Large single-spin asymmetries at CM energies of 20 and 200 GeV
- **Weren't supposed to be there** in naïve pQCD
- May arise from the Sivers effect, Collins effect, or a combination

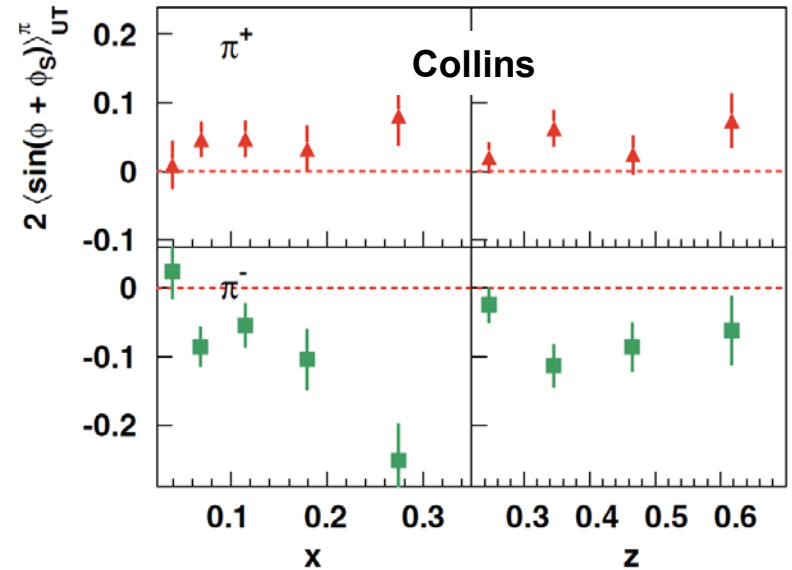
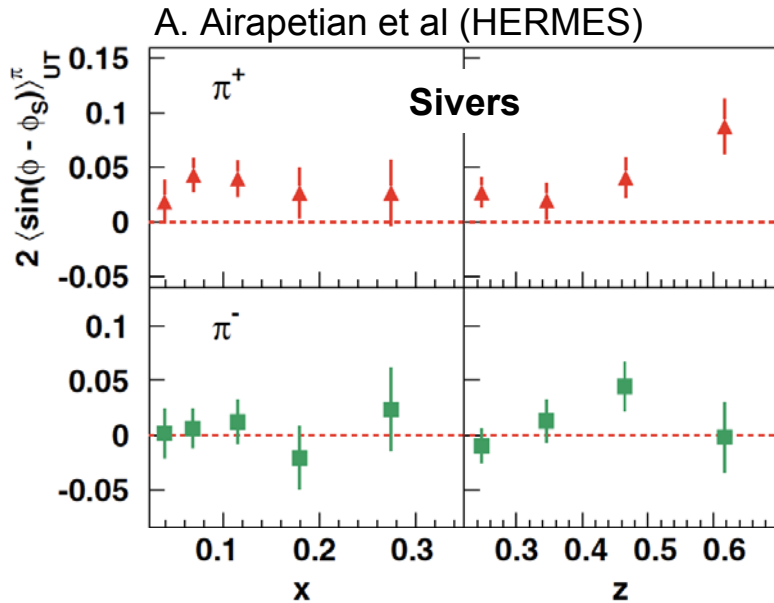
$$A_N \propto a_S m_q / p_T$$

Parton orbital motion

Transversity

What makes the proton spin?

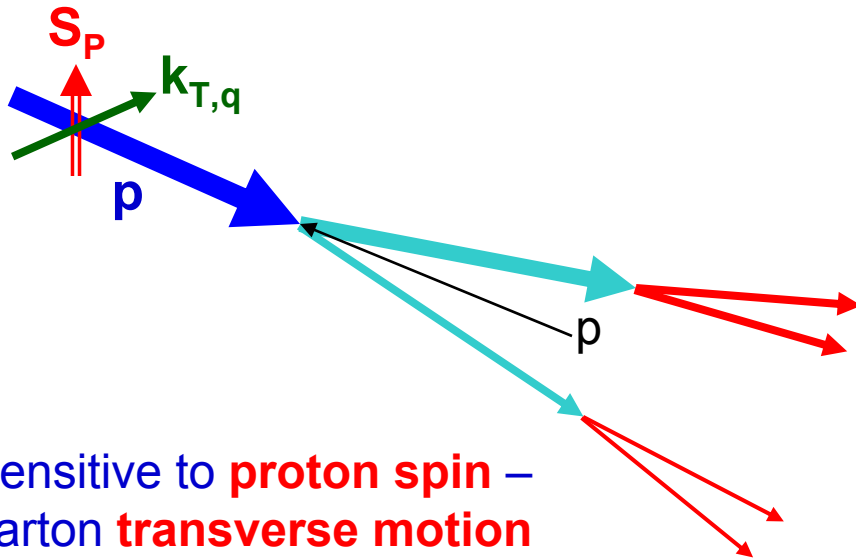
Sivers and Collins effects in deep-inelastic scattering



- Semi-inclusive DIS can distinguish the Sivers and Collins effects
- HERMES finds **both are non-zero**
- COMPASS finds consistent Collins effects; smaller Sivers effects

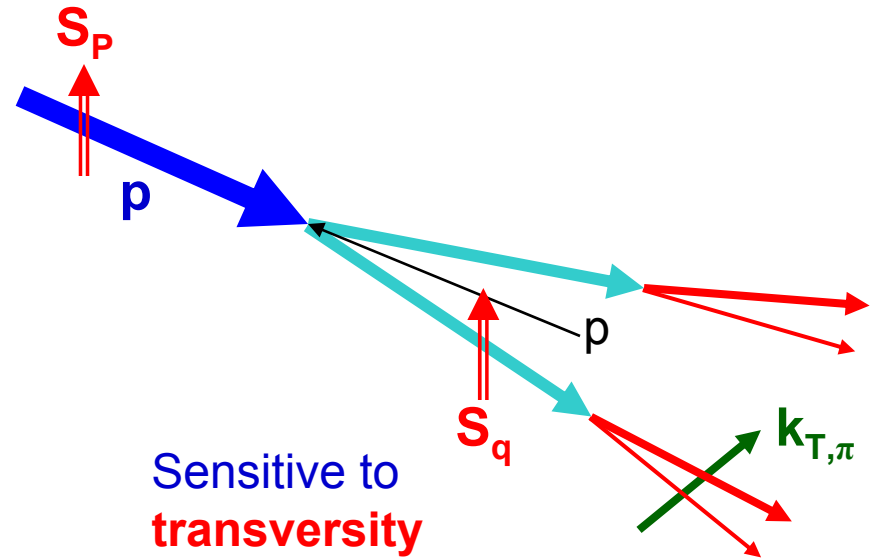
Sivers and Collins effects in pp collisions

Sivers mechanism: asymmetry in the forward jet production



Sensitive to **proton spin** –
parton **transverse motion**
correlations

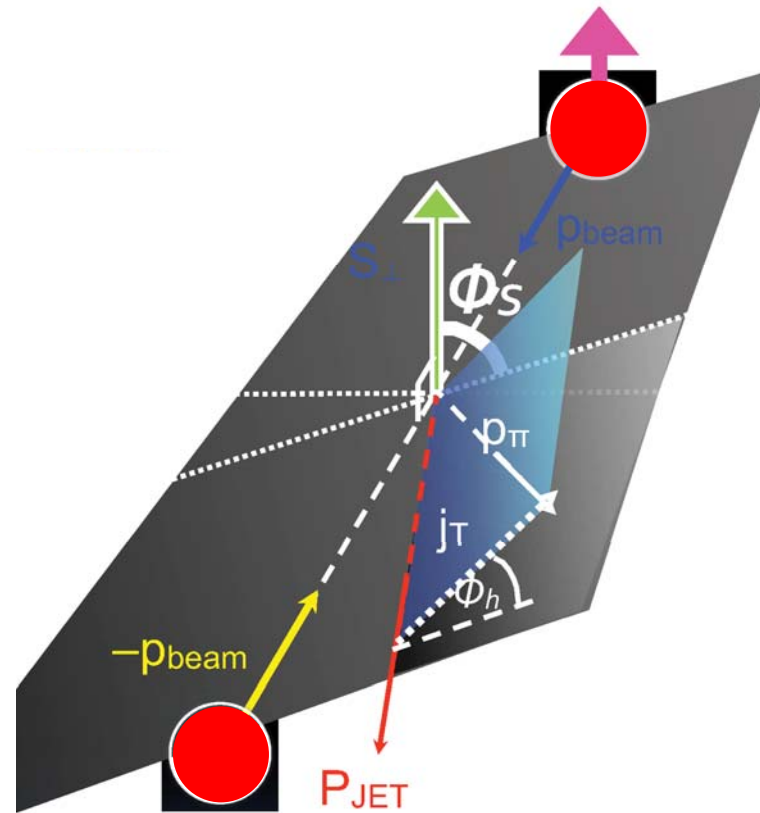
Collins mechanism: asymmetry in the forward jet fragmentation



Sensitive to
transversity

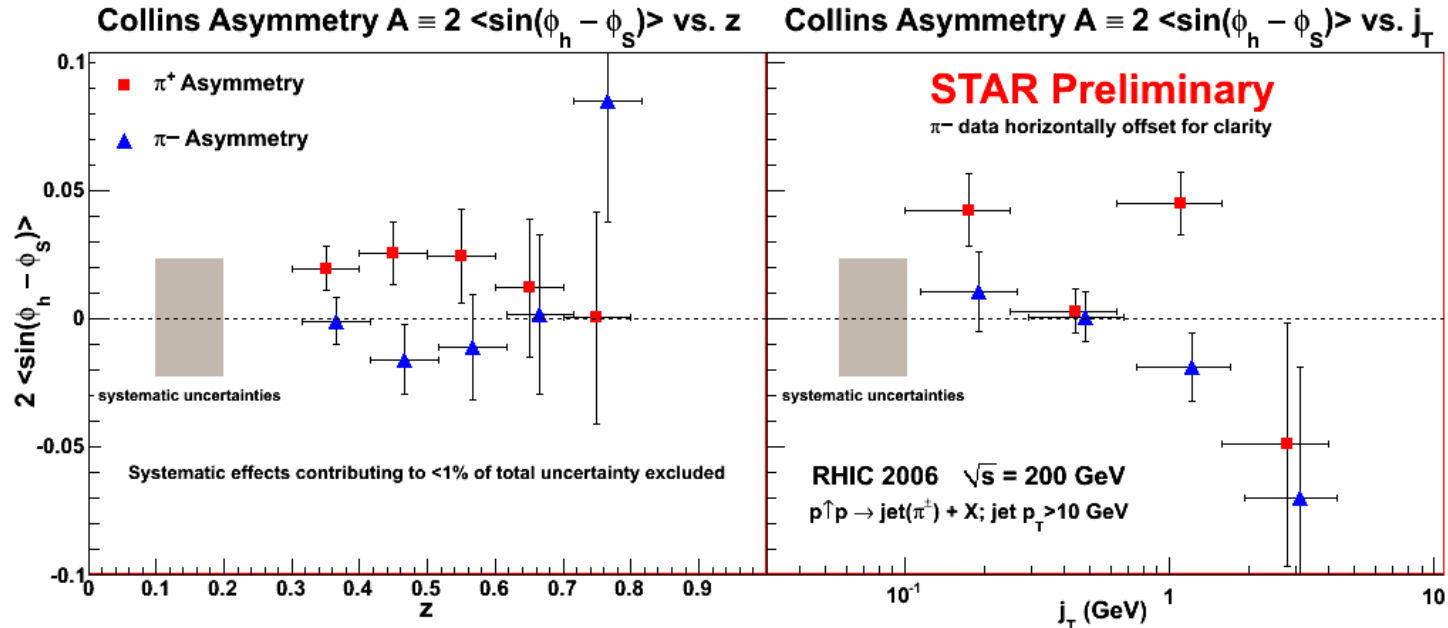
- Need to go **beyond inclusive hadrons**
- Limited (no more?) time: focus on **jet measurements of transversity**

Observing the Collins effect in jets



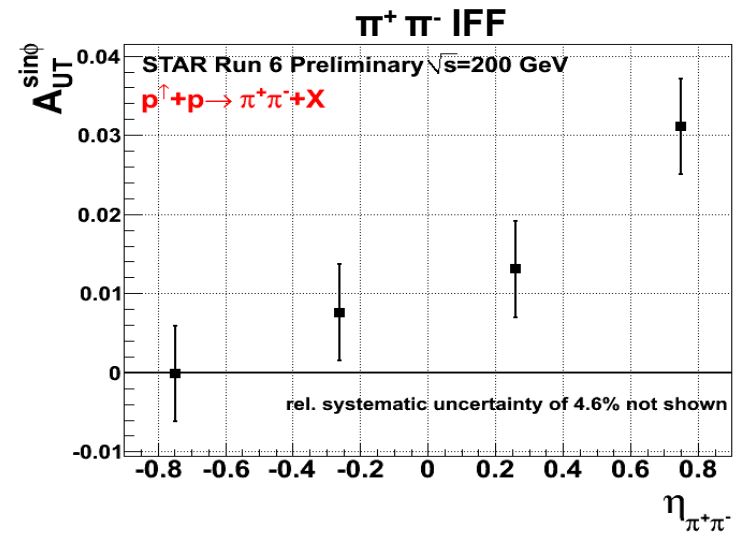
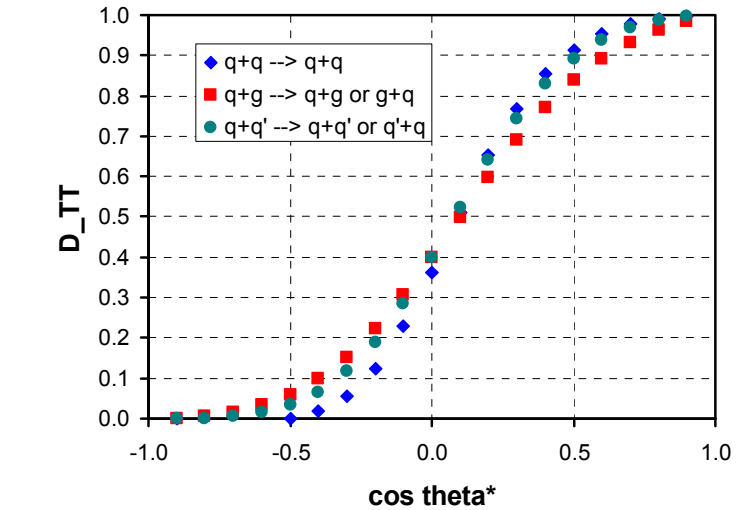
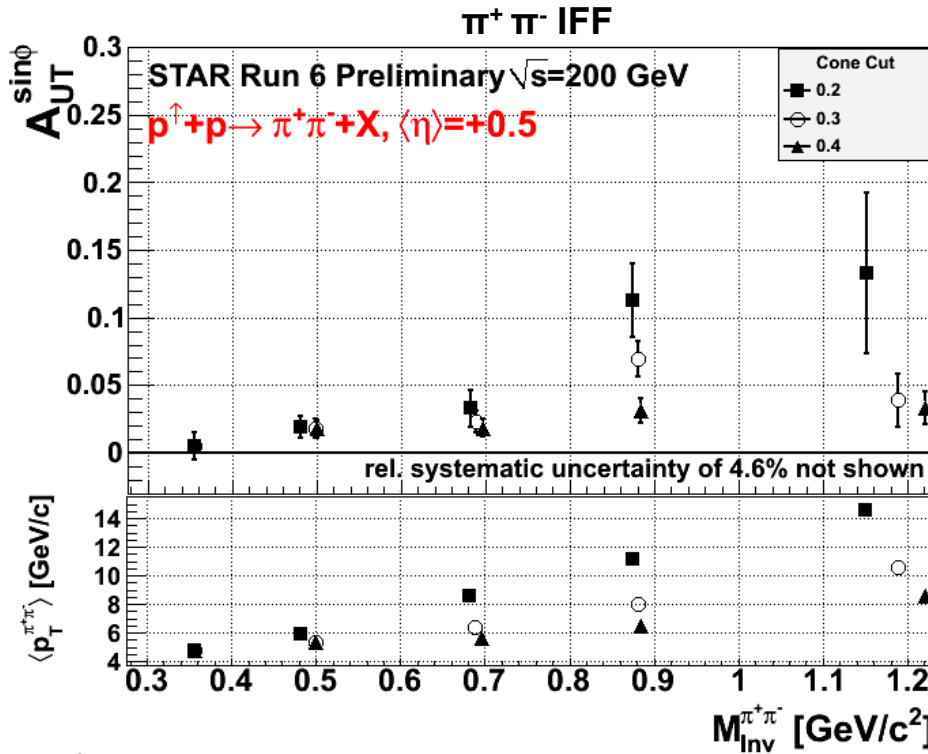
- A spin-dependent azimuthal variation in hadron production around the jet thrust axis
- Alternative approach: Interference Fragmentation Function (IFF)
 - Di-hadron as surrogate for the jet
 - Examine di-hadron relative angle, measured around the pair momentum

Leading pions in mid-rapidity jets



- Azimuthal asymmetries measured within fully reconstructed jets
- Average asymmetries:
 - $\pi^+ = 0.021 \pm 0.006 \pm 0.023$
 - $\pi^- = -0.004 \pm 0.007 \pm 0.023$
 - Expected asymmetry from global analysis $\sim \pm 0.07$

Mid-rapidity interference fragmentation functions



- Clear signature of quark transversity in p+p collisions at RHIC

Conclusions

- We still have a great deal to learn about the structure of the proton
- **RHIC is making significant contributions** to three poorly constrained pieces of the puzzle
 - **Gluon polarization**
 - **Flavor-separated quark and anti-quark polarizations**
 - **Transversity**
- Andrew will have more to say about gluon polarization in his, “What I did during my summer vacation,” talk. **Stay tuned!**